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NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

SIMTBED a Graphical Test Bed for Analyzing and Reporting the Results of a Statistical Simulation Experiment

by

Hans-Walter Drueg
September 1983

Thesis Advisor:

P.A.W. Lewis

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

Serial Correlation Coefficient

A graphical test bed in which the results of a simulation experiment can be reported and analyzed is described. The test bed is based on the regression adjusted graphics and estimation methodology developed by Heidelberger and Lewis [Ref. 1] for regenerative simulation. From the graphics and associated numerics, the experimenter can summarize and see simultaneously relative properties, such as bias, normality and standard

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deviation, of several estimators of a characteristic of a population for up to 8 sample sizes. The evolution of these properties with sample size is also displayed. The graphics is supported on a line printer to make it and the program portable. The technique is illustrated by examples concerning the effects of changes in data distribution on the behavior of the lag one serial correlation coefficient, the estimation of the shape parameter of Gamma random variables and a comparison of different methods (jackknife, bootstrap) for estimating the standard error of an estimator.



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SIMTBED a Graphical Test Bed for Analyzing and Reporting the Results of a Statistical Simulation Experiment

by

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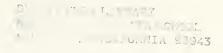
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ABSTRACT

A graphical test bed in which the results of a simulation experiment can be reported and analyzed is described. The test bed is based on the regression adjusted graphics and estimation methodology developed by Heidelberger and Lewis [Ref. 1] for regenerative simulation. From the graphics and associated numerics, the experimenter can summarize and see simultaneously relative properties, such as bias, normality and standard deviation, of several estimators of a characteristic of a population for up to 8 sample sizes. The evolution of these properties with sample size is also displayed. The graphics is supported on a line printer to make it and the program portable. The technique is illustrated by examples concerning the effects of changes in data distribution on the behavior of the lag one serial correlation coefficient, the estimation of the shape parameter of Gamma random variables and a comparison of different methods (jackknife, bootstrap) for estimating the standard error of an estimator.



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I. SYNOPSIS

SIMTBED

THE PROGRAM:

Portable FORTRAN program using printer plot graphics (3 different program versions)

Program will run on:

IBM

VAX

IBM PC

etc.

ca. 900 lines of FORTRAN Code

Memory requirements:

SIMTBl 1 M Bytes

SIMTB2 1 M Bytes

SIMTB3 0.5 M Bytes

(may slightly differ with different type of estimator functions and subsample sizes)

PURPOSES:

- To explore the distribution of a statistical estimator
- To see how that distribution changes with sample size
- To compare that distribution with the distribution of competing estimators



THE USER SUPPLIES:

A. Optional Parameters:

NE(1),NE(2),...,NE(8) = Subsample Sizes (maximum is 8)
The estimator is computed based on NE(i) data points

N = Total Number of simulated data points per replication

At Subsample Size NE(i), there are [N/NE(i)] independent values of the estimator

- M = Number of Replications
 When all replications have been run, there are
 M*[N/NE(i)] independent values of the estimator
 at each NE(i)
- D = Degree of Regression (maximum D = 3)
- L = Number of Subsample Sizes (maximum L = 8)

 GRAPHICS and SCALING options

B. Data:

A total of M*N simulated data values are needed. In SIMTBl and SIMTB2 the same data is used at each subsample size (NE(i)). In SIMTB3 new data is always generated.

C. Estimators:

Up to 3 FORTRAN functions (i.e. Estimators) are needed. They must accept as inputs a data subsample and the size of that subsample. They must return one value of the estimator for that subsample.



SIMTBED PRODUCES:

- A one page graphical output (box plots) at each subsample size
- Numerical Summaries at each subsample size (mean, Std. Dev., Std. Dev. of the mean, skewness, kurtosis)
- Regressions to quantify changes in the mean and variance as subsample size changes



II. INTRODUCTION

and SIMTBED, with the different versions (SIMTB1, SIMTB2 and SIMTB3) is a graphical display program. The program is based on the program RAGE [Ref. 2]. It is used, with simulated data, on a digital computer. The program can be used to examine statistical estimators of different type, or properties of a single estimator under different distributional assumptions. The distribution of the estimator can be explored for given sample sizes and the properties can be compared for different sample sizes. The estimation conditions are controlled by the experimenter. It is also possible to examine the effects of changes in the underlying distribution of the data.

When the program SIMTB1 or SIMTB2 is used with simulated data, the data is assumed to be independent and identically distributed (iid). This iid data can be sectioned into M independent blocks of specified sample size N. The sample of size N, will be sectioned into smaller subsample of size NE(k). The estimates are then calculated from this subsample of size NE(k).

One salient feature of the program versions SIMTBl and SIMTB2 is that they use the same batch of simulated random variables to explore the properties of all the estimators at the various subsample sizes. This is done for economy



and could be important on slow computers; the price paid is that the regression analysis provided by SIMTB1 and SIMTB2 of its graphical output is performed on correlated samples.

The version SIMTB3 uses one dimensional data and does not have this repetition feature. New data is used for each calculation of each estimator at each subsample size. The data is generated when the estimator function is called and only the needed batch of the exact subsample size is generated. This technique reduces the memory requirements.

Moreover all data sets are uncorrelated and a much more precise correlation can be performed if required. But this technique increases the computer time.

To use the program it is necessary only to define the optional parameters (see Section IV), supply the simulated random variables or a batch of data points, and provide the FORTRAN functions for the calculation of the estimators which are of interest. The program itself will subdivide the input data and feed the data properly into the functions, scale the graphic display, produce boxplots and summary statistics. A regression will be computed for the mean and variance of each estimator based on inverse subsample size. The result of the regression is displayed graphically and numerically.

The program is written in ANSI Standard FORTRAN (X3.9-1966) and extensively tested on an IBM 3033 computer using FORTRAN IV (H Extended) or FORTRAN IV (G1) compilers. The



program SIMTBED (all versions) provides all subroutines used inside the program. Besides the estimator functions, the user has to provide NO additional subroutines via packages like IMSL. The program should be totally portable; it has been tested under FORTRAN 77 on a VAX 11/780. The only limitation is the available memory.



III. GENERAL IDEA AND DATA STRUCTURE OF THE PROGRAM

The main purpose of SIMTBED, with the different versions, is to explore the distributional behavior of estimators and show their properties in a graphical and numerical display. All versions use the same ideas, they only differ in the type of data and the way the data is used inside the program.

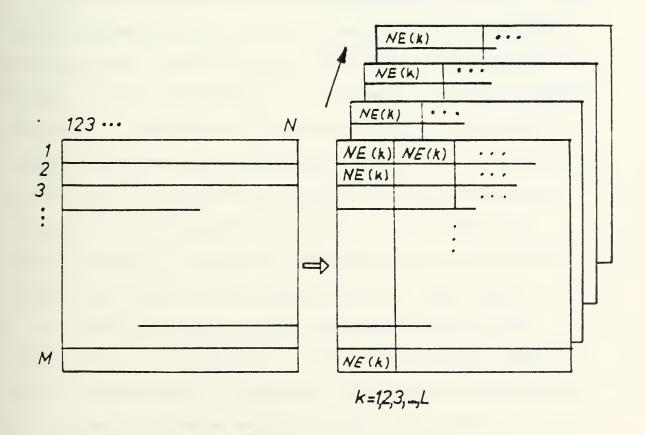


Figure 1. Sectioning of the Data into M*N Sections



To study the behavior of an estimator the experimenter usually uses well known simulated data. Thus if one is interested in exploring the behavior of estimates of the shape parameter in a Gamma population, one generates Gamma variates from a random number generator package (e.g., IMSL subroutine Chap. G). This batch of simulated data is processed by SIMTBED in the following way.

The data batch is first divided into M independent blocks. Each block contains N data points. So the starting data batch has to consist of M*N data points (see Figure 1).

All blocks are divided into subsamples of size n_i . The actual subsample size n_i is an element of the subsample size array NE. This array can store up to 8 different values. Then the estimator is calculated for each subsample of size n_i . The estimator function will be calculated $(\lfloor N/n_i \rfloor)$ *M times. This total population of estimates is used to evaluate the summary statistics for the estimate and construct the corresponding box plot. If NE contains another element, the blocks are divided into the new subsample n_{i+1} size and all calculations are done again.

In addition to the summary statistics and the box plots (see e.g., Figure 3a), a regression on the averages and on the variance is computed, following the methodology of regression adjusted estimate (RARE) developed by Heidelberger and Lewis [Ref. 1].



The RARE estimate is the regression coefficient α_0 . It is the asymptotic estimate of the expected value of the parameter. The unbiased RAGE estimate of the average of the parameter is determined by the regression formula:

$$E(\theta(n_i)) = \alpha_0 + \alpha_1 \frac{1}{n_i} + \alpha_2 \frac{1}{n_i^2} + \dots + \alpha_D \frac{1}{n_i^D}$$

where D is an input parameter.

The asymptotic RARE estimate is printed as a dashed line in the graph.

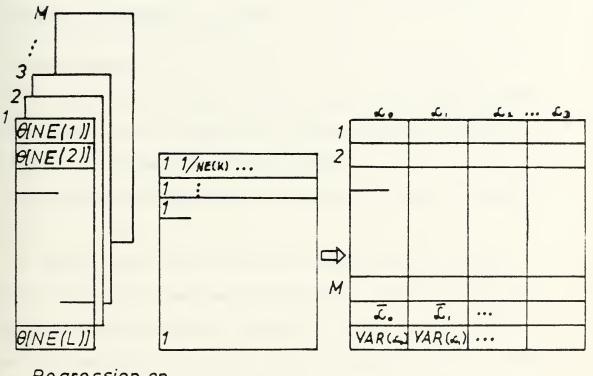
The unbiased RAGE estimate of the variance of the estimator is given by the formula:

$$s^{2}(n_{i}) = \beta_{1} \frac{1}{n_{i}} + \beta_{2} \frac{1}{(n_{i})^{1.5}} + \beta_{3} \frac{1}{(n_{i})^{2}} + \dots$$

The regression calculations of the average are done for each block separately. The result are M sets of regression coefficients. The finally printed regression coefficients are the averages of the M replications (see Figure 2). From the set of coefficients the variance and the standard deviation of the regression coefficients is calculated.

The regression on the variance is done once, using all (M*N) data points.





Regression on

Figure 2. Structure of the Regression Coefficients



IV. ARGUMENTS OF THE PROGRAMS SIMTB1 AND SIMTB2

All versions of SIMTBED have in general the same argument list. SIMTB2 (a version for multivariate random variables) has two additional arguments. All arguments will be described in detail and all restrictions or limitations will be discussed. In Section V, detailed examples of setups for SIMTB1 and SIMTB2 are given.

A. X--DATA ARRAY

The array X is the input data array. X is single precision REAL*4, and is generally simulated data e.g., in Section VII, independent Gamma variates.

In SIMTBl the dimension of the array X must not exceed 50,000.

In SIMTB2 the input data is multivariate and consequently the array X has two dimensions. The size of the dimensions is not directly limited by the program. The space must be provided by the calling program and is passed as an argument (see IR and IRK). The memory requirements increase rapidly as the dimensions of X increase.

B. N--SAMPLE SIZE

The sample size N is the number of data points per section of input data X. N is an INTEGER. Depending on the precision of the simulation that is required, the sample size N can vary from 1 to 50,000.



In SIMTB2 N is the number of multivariate data points per section. M (the number of replications) times N must not exceed IR, the row dimension of X.

If M times N exceeds 50,000 an error message will be printed and the execution will be terminated. If the product M times N exceeds the total number of data points provided by the user, NO error message will signal the user error and the result of the execution is not predictable.

C. M--NUMBER OF REPLICATIONS

The number of replications M of the array X is an INTEGER. M determines the number of sections, into which the data set X is divided. So M*N is the dimension of X in SIMTB1. The parameter M also determines the number of regressions on the mean values that will be run to find the regression coefficients in the regression on the mean. If M is 1 only one regression will be done and no variance and standard deviation of the regression coefficients can be calculated.

D. NE--SUBSAMPLE SIZE ARRAY

The argument NE is an INTEGER array, containing up to 8 subsample sizes. These are the subsample sizes at which the properties of the estimator are to be investigated. NE must always contain 8 elements. If less than 8 subsample sizes are used, the array must be filled up with dummy values. The estimator is calculated for each subsample



individually. The used values of NE (not the dummy values) have to be ordered from the smallest to the largest (NE(1) < NE(2) < NE(3) < ...).

The program can only handle up to a total number of 12,500 estimates. This limit is caused by storage limitations and can be expanded for larger computers. The smallest subsample size NE(1) produces the most estimates and if this case exceeds 12,500 the execution will be terminated and an error message will be printed.

In SIMTB2 all values of NE have to be less than 5,000.

E. L--NUMBER OF SUBSAMPLE SIZES (BOX PLOTS)

The number of box plots L in the graphical output (the number of subsamples at which the estimator is examined), is an INTEGER with values from 1 to 8. The value of L determines how many elements of the array NE the program will use (e.g., L = 2, the program uses only NE(1) and NE(2) for the calculations). L determines the number of box plots and the number of corresponding summary statistics in the output. If L is out of range the program will terminate execution and print an error message.

For L = 1 no regression is possible. No regression output will be printed.

F. D--DEGREE OF REGRESSION

The degree of regression on the mean D, is an INTEGER with values from 1 to 3. The chosen degree refers to the



number of coefficients calculated and printed for the regression equations. Experience has shown that D=3 is preferable (higher values cause severe numerical problems in the regression computations).

If D exceeds the value of L-1, the program reduces D to this number, regardless of the value chosen by the user.

G. RG--REDUCED GRAPHICS

The argument RG is an INTEGER with value:

0 = off ==> full graphics

l = set ==> reduced graphics

In the reduced graphics case the vertical scale of the graph is reduced by eliminating the outliers. Only the number of outliers is counted and the number is printed.

This enables the user to see the body of the boxplot in more detail.

H. SEI--SCALING ESTIMATORS INDIVIDUALLY

The argument SEI is an INTEGER with value:

0 = off ==> common scaling

l = set ==> individual scaling.

For SEI = 0 all printed graphs (max. 3 per program run) are scaled to the same range. This makes the comparison of the different graphs easier. The value SEI = 1 causes the program to scale each graph individually.

The argument SEI works in combination with the arguments RG and SVS. The combination of these three arguments make it possible to fit the printed graphs to the needs of the user.



- I. SVS--SETTING THE VERTICAL SCALE

 The argument SVS is an INTEGER with value:
- 0 = off ==> automatic scaling
- 1 = set ==> scaling by the user.

SVS = 0 causes the program to calculate the scale of the graphic printout. The final graphic display is influenced by the chosen values of RG and SEI. The values of YMIN and YMAX are ignored by the program.

For SVS = 1 the user must provide the scaling. The graphics are vertically scaled to a given minimum value (YMIN) and maximum value (YMIN and YMAX). The arguments of RG and SEI are ignored. Only the numbers of outliers outside the display are printed for each box plot.

J. YMIN--MINIMUM VALUE OF THE VERTICAL SCALE

The scaling parameter YMIN is data type REAL*4. It is the lower limit of the vertical scale. It affects the scaling only in combination with SVS = 1. If the chosen value is so large that the value YMIN lies inside the body of the box plot, an error occurs and the program ends with an abnormal ending.

K. YMAX--MAXIMUM VALUE OF THE VERTICAL SCALE

The scaling parameter YMAX is data type REAL*4. It is the upper limit of the vertical scale. The scaling is only effected if SVS has value 1. If the value of YMAX is too small and it lies inside the body of the box plot, the program comes to an abnormal ending.



YMIN and YMAX in combination with SVS = 1 should only be used for well known graphic ouptut. With this option, it is possible to scale the output of different program runs to a common scale. In particular if more than 3 estimators have to be estimated and compared, so that a common scale is needed, this option may be used.

L. NEST--NUMBER OF ESTIMATORS

The parameter NEST is an INTEGER with the value 1, 2 or 3. The value of NEST determines the number of different one-page graphic displays the program produces with one call from the calling program. Usually the value of NEST is equal to the number of different estimators used in the program.

In SIMTB2 the same estimator may be used with different (e.g., normal, exponential etc.) distributed data sets.

M. EST1, EST2, EST3--ESTIMATOR FUNCTIONS

These 3 parameters are data type REAL*4 and are used to pass the EXTERNAL function names to the program. An external declared function is a function which computes the value of an estimator. This function may call other routines, but the final value of the estimator must be passed over this function name.

For SIMTBl each function must have the two arguments X and NEK (e.g., FUNCTION VARIANCE (X,NEK)). X is the data array and NEK is the number of data elements in X.



SIMTB2 needs for each function four arguments X, NEK, IDR, IRK (e.g., FUNCTION CORRELATION (X,NEK,IDR,IRK)). X is a two dimensional data array and NEK is the subsample size, for which the function is evaluated. IDR and IRK are the dimensions of the array X.

If the user wants to use less than 3 estimator functions, he must use dummy arguments and choose the correct value of NEST. The easiest way to do this is to use a function of a previous used estimator again (for details of the programming see Section V).

N. TTL1, TTL2, TTL2--DESCRIPTION OF THE ESTIMATORS

These arrays are used to pass titles from the calling program to SIMTB. Each title has to be 120 characters long (15 fields, each 8 characters wide). The title is printed below the output of the corresponding function.

If the user uses less than 3 functions and titles, he has to use dummy arguments (for details see Section V).

If the titles are not in the correct format, corresponding to the FORMAT statement the program will not execute properly.

O. IR, IRK--DIMENSIONS OF THE ARRAY X

These arguments are used ONLY in SIMTB2. IR (row dimension) and IRK (column dimension) are INTEGERS and have to match the dimension of X in the calling program.

If the dimensions don't match, NO error message will be produced and the output is unpredictable. The error may not be obvious, and the ouput may look reasonable.



V. DUMMY EXAMPLES OF IMPLEMENTING SIMTB AND SIMTB2 INTO A DRIVER-PROGRAM

The following examples show how the programs SIMTBl or SIMTB2 can be implemented into a FORTRAN driver-program.

The only purpose of the examples is to clarify the FORTRAN implementation, to avoid programming errors by the user.

Additional comment lines are added to the program examples.

In the first example SIMTBl is used to compare two different estimators (VAR and UNBVAR) of the variance of a normal sample. The sample may be generated with a random number generator (e.g., LLRANDOMII).

In the second example SIMTB2 is used to compare the distribution of two estimators. The estimators are the covariance (COV) and the correlation coefficient (CORR) of a bivariate standard normal sample.

- A. EXAMPLE 1 USING SIMTB1
 MAIN
- C EXAMPLE of SIMTBl Calling program, it has not to be the MAIN program

REAL*4 X(50000), YMIN, YMAX, VAR, UNBVAR

REAL*8 T1(15), T2(15), T3(15)

INTEGER N, M, NE(8), L, D, RG, SEI, SVS, NEST

C

DATA N /2500/



```
DATA M / 20/
     DATA NE /10,20,25,50,100,0,0,0/
  Array NE must have 8 elements, if only 5 are used, add
C
   dummy variables and set L = 5
C
    DATA L / 5/
    DATA RG / 0/
    DATA SEI / 0/
    DATA SVS / 0/
    DATA NEST/ 2/
    DATA T1 /'ESTIMATE','OF THE V','ARIANCE','USING ',
   +'VAR=(1/N)','*SUM(X(I',')-XBAR)*','*2 ',7*''/
    DATA T2 /'ESTIMATE','OF THE V','ARIANCE ','USING ',
   +'VAR=(1/(1','-N))*SUM','(X(I)-XB','AR)**2 ',7*' '/
C
  All 15 fields (each 8 characters) have to be
  initialized
C
C
    EXTERNAL VAR, UNBVAR
C
  Generate M*N independent Normal (0,1) Random numbers
C
C
  and store into X
C
    CALL SIMTB1(X,N,M,NE,L,D,RG,SEI,SVS,YMIN,YMAX,NEST
               , VAR, T1, UNBVAR, T2, VAR, T1)
  EST3=VAR and TTL3=Tl used as dummy variables
C
C
    STOP
    END
```



```
FUNCTION VAR (X, NEK)
C Function to calculate the Variance.
C All calculations inside the function should be done in
C DOUBLE PRECISION
C
    REAL*4 X(N), VAR
    REAL*8 SUM, XBAR, DVAR
C
    SUM=0.0D0
     DO 10 I=1, N
       SUM=SUM+DBLE(X(I))
     10 CONTINUE
       XBAR=SUM/FLOAT(N)
       SUM=0.0D0
    DO 20 I=1,N
        SUM=SUM+((DBLE(X(I)))-XBAR)**2
     20 CONTINUE
       DVAR=SUM/FLOAT(N)
       VAR=SNGL (DVAR)
C
        RETURN
        END
        FUNCTION UNBVAR (X, NEK)
C Function to calculate the Variance.
C All calculations inside the function should be done in
```

C



```
C
  DOUBLE PRECISION
C
     REAL*4 X(N), UNBVAR
     REAL*8 SUM, XBAR, DUNVAR
C
     SUM=0.0D0
     DO 10 I=1,N
        SUM=SUM+DBLE(X(I))
 10 CONTINUE
     XBAR=SUM/FLOAT(N)
     SUM=0.0D0
     DO 20 I=1, N
        SUM=SUM+((DBLE(X(I)))-XBAR)**2
 20 CONTINUE
     DUNVAR=SUM/FLOAT(N)
     UNBVAR=SNGL (DUNVAR)
C
     RETURN
     END
B.
   EXAMPLE 2 USING SIMTB2
   MAIN
 EXAMPLE of SIMTB2 Calling program, it has not to be
   the MAIN program
   REAL*4 X(25000,2), YMIN, YMAX, COV, CORR
   REAL*8 T1(15), T2(15), T3(15)
```



```
INTEGER N, M, NE(8), L, D, RG, SEI, SVS, NEST, IR,
   +
             IRK
C
     DATA N /2500/
     DATA M / 10/
     DATA IR /25000/
     DATA IRK / 2/
C
  IR and IRK must be equal to the dimensions of X
     DATA NE /10,20,25,50,83,100,125,250/
     DATA L / 8/
     DATA RG / 0/
     DATA SEI / 0/
     DATA SVS / 1/
     DATA YMIN/ 0.0/
     DATA YMAX/ 1.0/
     DATA NEST/ 2/
     DATA T1 /'ESTIMATE', 'OF THE C', 'OVARIANC', 'E',
    +11*' '/
     DATA T2 /'ESTIMATE','OF THE C','ORRELAT1','ON COEFF',
    +'ICIENT ','10*' '/
  All 15 fields (each 8 characters) have to be
C
  initialized
C
C
    EXTERNAL COV, CORR
C
C
  Generate M*N pairs of independent random bivariate
C
  numbers, each pair being independent N(0,1) random
```



```
C
   variables and store into X
C
      CALL SIMTB2 (X,N,M,NE,L,D,RG,SEI,SVS,YMIN,YMAX,NEXT
                   ,COV,T1,CORR,T2,COV,T1,IR,IRK)
C
    EST3=COV and TTL3=T1 used as dummy variables
C
      STOP
      END
C
C
      FUNCTION COV (X, NEK, IDR, IRK)
C
    Function to calculate the Covariance.
    All calculations inside the function should be done in
C
C
    DOUBLE PRECISION
C
      REAL*4 X(IDR, IRK), COV
      REAL*8 SUM1, SUM2, SUM3, XBAR1, XBAR2, EX1X2, DCOV
C
      SUMl=0.0D0
      SUM2=0.0D0
      SUM3=0.0D0
      DO 10 I=1, N
         SUM1=SUM1+DBLE(X(I,1))
         SUM2=SUM2+DBLE(X(I,2))
         SUM3=SUM3+DBLE(X(I,1)*X(I,2))
   10 CONTINUE
      XBAR1=SUM1/FLOAT(N)
```



```
XBAR2=SUM2/FLOAT(N)
     EX1X2=SUM3/FLOAT(N)
     DCOV=EX1X2-(XBAR1*XBAR2)
     COV=SNGL (DCOV)
C
     RETURN
     END
C
     FUNCTION CORR (X, NEK, IDR, IRK)
   Function to calculate the Correlation coefficient
C
C
  All calculations inside the function should be done in
С
   DOUBLE PRECISION
С
     REAL*4 X(IDR, IRK), CORR
     REAL*8 SUM1, SUM2, SUM3, XBAR1, XBAR2, EX1X2, VAR1, VAR2,
            COV, DCORR
C
     SUM1=0.0D0
     SUM2=0.0D0
     SUM3=0.0D0
     DO 10 I=1,N
        SUM1=SUM1+DBLE(X(I,1))
        SUM2=SUM2+DBLE(X(I,2))
        SUM3=SUM3+DBLE(X(I,1)*X(I,2))
 10
     CONTINUE
     XBAR1=SUM1/FLOAT(N)
```



```
XBAR2-SUM2/FLOAT(N)
     EX1X2=SUM3/FLOAT(N)
     SUM1=0.0D0
     SUM2=0.0D0
     DO 20 I=1,N
        SUM1=SUM1+DBLE(X(I,1)**2)
        SUM2=SUM2+DBLE(X(I,2)**2)
 20
     CONTINUE
     VAR1=(SUM1/FLOAT(N))-(XBAR1**2)
     VAR2 = (SUM2/FLOAT(N)) - (XBAR2**2)
     COV=EX1X2-(XBAR1*XBAR2)
     DCORR=COV/((VAR1*VAR2)**0.5)
     CORR=SNGL (DCORR)
C
     RETURN
```

END



VI. STUDY OF THE BEHAVIOR OF SERIAL CORRELATION ESTIMATES FOR DIFFERENT DISTRIBUTIONS

CALCULATION OF THE FIRST SERIAL CORRELATION COEFFICIENT Α. It is known that for an independent sample from a population with finite variance, the distribution of the serial correlation coefficient (Anderson and Walker, 1964) [Ref. 3] is asymptotically Normal with mean zero and variances 1/n, where n is the sample size. If the population is i.i.d Normal then the bias is exactly -1/n. Since those asymptotic properties are frequently used as approximations in tests of significance, it is important to know how valid the approximation would be in small samples from a variety of distributions. We will look at that question in the next two sections and then go on to consider two alternative measures of correlation, Fisher's z-transform and the 2-fold jackknifed estimate of the correlation. Their ability to reduce bias and/or induce Normality will be examined against other changes in the distribution of the estimators, particularly variance inflation. A simulation study, without

B. SIMTB1 OUTPUT FOR SERIAL CORRELATION

(1966) [Ref. 4].

Figure 3(a) shows the simulated distribution and sample properties of the serial correlation coefficient estimate

graphics, of some of these problems was conducted by Cox



$$r_{n} = \frac{\sum_{j=1}^{n-1} (x_{j} - \overline{x}_{1})(x_{j+1} - \overline{x}_{n})}{(n-1) \sum_{j=1}^{n} (x_{j} - \overline{x}_{0})^{2}},$$

where:

$$\overline{X}_0 = \int_{j=1}^n X_j/n,$$

$$\overline{X}_1 = \int_{j=1}^{n-1} X_j/(n-1), \text{ and}$$

$$\overline{X}_n = \sum_{j=2}^n X_j/(n-1)$$

for various sub-sample sizes $n=n_1$. This definition matches that used by Anderson and Walker (1964). We consider first subsamples of size $n_1=10$, and then of size $n_2=20$, $n_3=30$, $n_4=40$, $n_5=50$, $n_6=75$, $n_7=100$ and $n_8=150$, successively. For each subsample size the input sample of N=5000 simulated Normal (0,1) random variables is divided into as many full subsamples of size n_1 as possible, and the serial correlation is computed for each of the $\lfloor N/n_1 \rfloor$ subsamples of size n_1 . The entire procedure is then replicated M=10 times, each time with a new simulated sample of N=5000 Normal (0,1) variables.

After all M replications have been run, all the estimates of serial correlation for each subsample size are grouped together and their simulated distribution is presented via a



boxplot and summary statistics. The boxplot follows the standards discussed in Mosteller and Tukey (1977) [Ref. 5] with the median denoted by a + within the box, the mean by a * within the box, the outliers by 0's, and the far outliers by *'s beyond the whiskers. The summary statistics include the sample mean, sample standard deviation, estimated standard deviation of the sample mean (i.e., sample standard deviation/ $\text{sqrt}(M[N/n_{\dot{1}}])$, sample skewness and sample kurtosis of the correlation estimates.

Looking at the output, the first (leftmost) boxplot in the graph in Figure 3(a) shows the distribution of

(# Replications)
$$\times \left[\frac{\text{(Simulation Size)}}{\text{(Subsample Size)}} \right] = 10 \times \left[\frac{5000}{10} \right]$$

$$= 10 \times 500 = 5000$$

estimates of serial correlation from independent subsamples of size n_1 = 10. Summary statistics for the boxplot can be found below the graph in the column labeled "Subsample Size 10," so that the average serial correlation is -.1074, and the estimated standard deviation is .2996. The estimated standard deviation of the serial correlation estimate is .2996/ $\sqrt{(5000)}$ = .00424. Recall that this refers to correlation estimates based on subsamples of size 10.

Since the X-axis of the graph represents subsample size, the last (rightmost) boxplot shows the distribution of



$$10 \times \left| \frac{5000}{150} \right| = 10 \times 33 = 330$$

estimates of serial correlation from independent subsamples of size $n_8 = 150$. Although the 330 estimates are independent of each other, they are not independent of the 5000 estimates that comprise the first boxplot since the same data (divided and processed in different ways) was used for both. Summary statistics show that the average correlation has dropped to -.007372, indicating the fall off in bias, and the standard deviation has dropped to .07822, indicating the greater accuracy with which the correlation can be estimated when 150 points, rather than 10, are available.

In order to quantify the changes that are occurring in the mean and variance of the distribution of the estimator as subsample size changes, SIMTBl performs two types of regressions. The first regression is on the averages and is done after each replication, using the average serial correlation for that replication, \overline{r}_n , as the dependent variable. Inverse powers of the subsample size serve as the independent variables. For Figure 3(a) the degree of the regression was chosen to be D = 3 so, for each replication, the equations we attempt to fit by least squares are:

$$\overline{r}_{n_i} = a_0 + \frac{a_1}{n_i} + \frac{a_2}{n_i^2} + \frac{a_3}{n_i^3}$$
 for $i = 1, 2, ..., 8$.

This form anticipates the general asymptotic expansion



$$E(\widehat{\Theta}(n)) = \Theta + \frac{\alpha_1}{n} + \frac{\alpha_2}{n^2} + \frac{\alpha_3}{n^3} + \dots$$

which holds true in the current situation with $\Theta=0$ and (in the Normal case) $\alpha=-1$ (see Cramer (1948) for general results of this type) [Ref. 6].

Values of a_0 , a_1 , a_2 , and a_3 are calculated after each replication, averaged across the M replications to get \overline{a}_0 , \overline{a}_1 , \overline{a}_2 , and \overline{a}_3 , and then the averages are reported below the summary statistics on the line "Mean of Regression on Averages--Coefficients." We find that $\overline{a}_0 = -.000272$ and $\overline{a}_1 = -1.03074$, both close to their theoretical counterparts.

Because we have 10 replications and therefore 10 independent values of each of a_0 , a_1 , a_2 , and a_3 , we can also estimate the variances and standard deviations of a_0 , a_1 , a_2 , and a_3 across replications. These values are presented on the two lines immediately below the coefficients. For instance, the estimated s.d. of the estimate $\overline{a}_0 = -.000272$ of a_0 is .003892.

The regression line for the mean value of the estimator is presented visually in the graph as a dotted curve. The estimated asymptote (i.e., \overline{a}_0) is printed with a dashed line wherever it does not coincide with the regression line. Bias, therefore, can be viewed as the difference between those two lines.

The second regression referred to above is done after all replications have been run and the variances of the estimators



at each subsample size have been calculated. (Note that the standard deviations, not the variances, are presented in the summary statistics.) It should be recalled from previous discussion that these variances, as well as all measures in the summary statistics, are based on the grouping together of the serial correlations from all replications, at each subsample size. This is in contrast to the procedure for the regression on the means, where average correlations are computed for each subsample size for each replication. In the case of the variances, we have 8 equations:

$$\hat{\text{Var}}(r_{n_i}) = \frac{b_0}{n_i} + \frac{b_1}{n_i^{3/2}} + \frac{b_2}{n_i^2} + \frac{b_3}{n_i^{5/2}}, \quad i = 1, 2, ..., 8,$$

which we fit by least squares in order to estimate the coefficient β_0 , β_1 , β_2 , and β_3 in the presumed asymptotic expansion

$$Var(\hat{\Theta}(n)) = \frac{\beta_0}{n} + \frac{\beta_1}{n^{3/2}} + \frac{\beta_2}{n^2} + \frac{\beta_3}{n^{5/2}} + \dots$$

This expansion holds for the variance of the estimated serial correlation coefficient for independent data. Usually it will be β_0 in which we are most interested since β_0 is used in computing asymptotic relative efficiencies of estimators. For independent data with finite variance, we know that β_0 = 1. The computed values of b_0 , b_1 , b_2 , and b_3 , are presented on the line labeled 'Regression on Variance-- Coefficients'. Notice that b_0 = .7438 is close to the theoretical value of 1.



The final two numbers on Figure 3(a), YMIN and YMAX, simply show the scale of the vertical axis. Because the SIMTB1 program option to put Figures 3(a), 3(b) and 3(c) on the same scale was in effect, it may be that no boxplot in a given Figure (e.g., Figure 3(b)) requires the full range of Y-values.

In order to produce Figure 3(b), the Normal (0,1) data that went into Figure 1(a) was squared to create longer tailed $\chi^2(1)$ random variables. The output is entirely analogous to that for Figure 3(a). Similarly, for Figure 1(c), the Normal (0,1) data was exponentiated in order to create Lognormal (0,1) data and to produce analogous graphical output. The indication is that the distribution of the sample serial correlation is robust with respect to the population distribution.

The features of the SIMTBl output will become clearer when they are associated with the various properties of the correlation estimator. First, however, a few technical comments concerning the regressions are necessary.

C. SOME COMMENTS ON THE REGRESSIONS

Two types of problems, numerical and statistical, can occur when attempting to fit the two sets of regression equations presented in Section VI.B.

First, there is the question of numerical stability when the independent variables, $\{1, n_i^{-1}, n_i^{-2}, n_i^{-3}\}$ or $\{n_i^{-1}, n_i^{-3/2}, n_i^{-2}, n_i^{-5/2}\}$ decrease geometrically. If we



attempt to form x^Tx , where x is the respective design matrix and x^T is the transpose of x, we get values that range from 8 (assuming 8 subsample sizes) to $\sum\limits_{i=1}^{8} n_i^{-6}$ for the regression on the means, and $\sum\limits_{i=1}^{8} n_i^{-2}$ to $\sum\limits_{i=1}^{8} n_i^{-5}$ for the regression on the variances. Experience has shown that attempts to solve systems with such extremes in the x^Tx matrix produce erroneous results. Instead, SIMTBl scales the design matrices by multiplying each column of x by $\max\limits_{i=1}^{8} n_i^{-2}$ raised to the proper power so that no entry becomes too small. The standard Choleski decomposition is then used to fit the equations, and the coefficients are properly rescaled before they are reported. This procedure produces numerically reliable results.

The second problem concerns the breakdown of statistical assumptions in our regression models. It has already been pointed out in Section VI.B that the two sets of dependent variables:

(1) the $\overline{\Theta}$ (n_i) when considering the regression on the means;

(2) the
$$s^{2}(n_{i}) = M \begin{bmatrix} N/n_{i} \end{bmatrix} \frac{(\widehat{o}_{j}(n_{i}) - \overline{o}(n_{i}))^{2}}{M[N/n_{i}]}$$

when considering the regression on the variances, are not independent over i since all are based on the same simulated data. The extent of the dependence is demonstrated by the correlation matrix in Table 1. Entries in that table show the estimated correlation between $s^2(n_j)$ and $s^2(n_j)$ for



TABLE 1

ENTRIES IN THE TABLE ARE THE ESTIMATED CORRELATIONS BETWEEN THE ESTIMATED VARIANCES OF THE r AT DIFFERENT SUBSAMPLE SIZES:

$$CORR(s^{2}(r_{n_{j}}), s^{2}(r_{n_{j}}))$$
 for $i = 1, ..., 8, j = 1, ..., 8$

	i	1	2	3	4	5	6	7	8	
j										
1		1.00	.49	.46	26	.18	17	.14	.01	
2		.49	1.00	.40	.55	.11	.38	.38	03	
3		.46	.40	1.00	.23	.23	.44	.21	. 29	
4		26	.55	.23	1.00	.42	.86	.57	.35	
5		.18	.11	.23	.42	1.00	.71	.43	.59	
6		17	.38	.44	.86	.71	1.00	.45	.53	
7		.14	.38	.21	.57	.43	.45	1.00	.72	
8		.01	03	.29	.35	.59	.53	.72	1.00	

Recall that r_n is the estimated serial correlation for a simulated Normal (0,1) subsample of size n. Also, the estimated correlations shown above were computed using 10 values (replications) of $s^2(r_n)$ and $s^2(r_n)$ for each i and j.



all i and j, where the estimation was done by repeating the SIMTBl experiment with 10 different batches of 50,000 simulated random variables. Since only 10 values went into each correlation calculation, the table is only accurate to within approximately $\pm 2/\sqrt{10} = .632$. We see some indication of positive correlation, especially when i and j are close, but the lack of independence is not severe enough to hurt the regression results for either the estimated means or variances significantly.

A second assumption, implicit in any regression, is that the dependent variables have equal variances. This condition holds true for the means, which can be shown to satisfy

$$Var(\overline{\Theta}(n_i)) = \frac{M}{N}$$

independently of i. The estimated variances, however, are not equivalent and, if we assume the $\hat{\Theta}_j$ (n_j) to be approximately Normally distributed so that

$$\begin{array}{ccc}
M \left[\frac{N}{n_{i}} \right] & (\hat{\Theta}_{j}(n_{i}) - \overline{\Theta}(n_{i}))^{2}
\end{array}$$

is approximately proportional to a χ_{M}^{2} $[N/n_{i}]-1$ random variable, we can compute

$$Var(s^{2}(n_{i})) = \frac{2}{MNn_{i}-n_{i}^{2}}$$



To correct this problem, SIMTBl scales the s $^2(n_i)$ by $\sqrt{n_i}$ so that

$$Var(\sqrt{n_i} s^2(n_i)) = \frac{2}{MN - n_i} = \frac{2}{MN}$$

since MN $>> n_i$. The design matrix is scaled accordingly and the values b_0 , b_1 , b_2 , and b_3 discussed in Section VI.B. are reported.

Table 2 shows the effects of the rescaling by presenting first the estimated variances of the $s^2(n_i)$, where the estimation is done by repeating SIMTBl for 10 batches of 50,000 simulated data points. These estimated variances decrease as n_i increases, closely paralleling the second line of Table 2 which has the approximate theoretical values (i.e., $2/(MNn_i - n_i^2)$). The final line of Table 2 shows the estimated variances of the rescaled $s^2(n_i)$, i.e., the $\sqrt{n_i}$ $s^2(n_i)$, which, as expected and hoped, show a more constant variance with i.

Although future versions of SIMTBl will include more sophisticated regression routines and the ability to generate independent samples at each subsample size, the SIMTBl is quick, usable, and accurate for most situations.

D. INTERPRETING THE SERIAL CORRELATION RESULTS

Returning to Figure 3(a) which shows the simulated distribution of the serial correlation coefficient from independent, Normal (0,1) data, the following comments summarize the most striking features:



TABLE 2

A COMPARISON OF THE ESTIMATED VARIANCE OF $s^2(r_n)$ WITH THE APPROXIMATE THEORETICAL VARIANCE OF n_i s $s^2(r_n)$ AND WITH THE APPROXIMATELY EQUIVARIANT SCALED VERSIONS, $n_i^{-.5}$ $s^2(r_n)$.

All entries have been multiplied by 10⁵.

n _i =	10	20	30	40	50	75	100	150
var(s ² (r _n))	.177	.150	.204	.079	.047	.031	.049	.022
Approx. Theoretical Var(s ² (r _n))	.400	.200	.133	.100	.080	.053	.040	.027
$\hat{\text{Var}}(n_{i}^{5} \text{ s}^{2}(r_{n_{i}}))$	1.77	2.99	6.12	3.18	2.33	2.33	4.88	3.35

The estimated variances of $s^2(r_n)$ and $\sqrt{n_i}$ $s^2(r_n)$ were calculated using 10 independent replications of $s^2(r_n)$.



- (a) The boxplots appear very symmetric at all subsample sizes with nearly equal numbers of outliers at either tail and with mean and median coincidental. This observation is confirmed by the estimates of skewness in the summary statistics. Kurtosis is mildly negative at small subsample sizes but, overall, asymptotic Normality seems to take hold rather quickly.
- (b) The average serial correlation is negative for small subsam-les. This is demonstrated by the dotted regression curve which starts at approximately -.10 and levels off near 0 for subsamples greater than about 85. The dashed asymptote of -.000272 is very close to the theoretical value of 0, and the mean values in the summary table closely reflect the bias of -1/n.
- (c) The standard deviations of the simulated distributions are very close to the asymptotic values of $n_1^{-0.5}$, although the lead coefficient in the regression on the variances, $b_0 = .743756$, is not as close to the theoretical value of 1 as we would hope. When SIMTB1 is repeated 10 times with 10 different batches of simualted data, we find an average value for b_0 to be 1.0604, with a standard deviation for b_0 of .307. The estimation procedure for b_0 , therefore, remains valid, but the estimate itself is highly variable.

The agreement between the simulated and the theoretical, asymptotic values of the bias and variances was discovered previously by Cox (1966). SIMTBl has now allowed us to



automatically look at a broader range of subsample sizes and to see, through boxplots and estima es of skewness and kurtosis, a fuller picture of any changes in the distribution of the estimator. We can be satisfied that estimates of serial correlation do behave approximately as Normal (-1/n, 1/n) rangome variables when the underlying data is Normal (0,1).

If the lead terms in the expansions of the mean and variance of the estimated correlation coefficient (i.e., a_0 , a_1 , and b_0) had been unknown, we would also have a fairly good idea now of what they were.

When the underlying data is χ^2_1 , Figure 3(b) confirms Cox's observation that the bias is relatively uneffected but, for small subsamples, the standard deviation is smaller than the expected $n^{-1/2}$. Unlike Figure 3(a), there is a pronounced skewness in the boxplots in Figure 3(b) with many more outliers at the positive end, and with the mean higher than the median at the first four subsample sizes. The problem of suppressed variance seems cured at $n_7 = 100$ and $n_8 = 150$, but the skewness remains and could cause problems in tests of significance.

Figure 3(c), which is based on an underlying batch of simulated Lognormal (0,1) data, shows a slight exaggeration of the effects in Figure 3(b). The standard deviation is more suppressed and does not attain the theoretical level by $n_8 = 150$. The positive skewness is more pronounced and kurtosis does not approach the theoretical value of 0.



Overall, the effects of long-tailed data on the distribution of the serial correlation coefficient can be summarized as follows:

- (i) Bias is not significantly effected and remains at approximately -1/n.
- (ii) The variance of the distribution of the serial correlation coefficient is reduced by longertailed data.
- (iii) Positive skewness is created in the distribution.
- (iv) Kurtosis may become positive at larger subsample sizes.
- (v) For long-tailed data (i.e., Lognormal), a subsample size of 150 is not large enough to insure asymptotic Normality.
- E. SIMTBL OUTPUT FOR THE Z-TRANSFORM OF THE CORRELATION Fisher's z-transform of the estimated correlated coefficient is defined by:

$$z_n = \frac{1}{2} \log \frac{1 + r_n}{1 - r_n}$$
,

where r_n is the estimated serial correlation presented in Section VI.B. The transformation is intended to make the distribution of the Z_n more Normal than that of the r_n . When the same SIMTBl experiment described in Section VI.B. is run using Z_n as the estimator instead of r_n , we get the results shown in Figures 4(a), 4(b) and 4(c). It should



be noted that the scale of the boxplots here has been forced to be approximately comparable to the scale for the boxplots in Section VI.B. This is done by suppressing outliers that are more than 1.5 interquartile distances beyond the quartiles of the boxplot. If we had allowed the data to scale the boxplots, we would have seen a much wider range on the vertical axis because the $\mathbf{Z}_{\mathbf{n}}$ are not restricted to the limits of -1 to +1 and because there is one far outlier at -3.8. In this type of "reduced graphics," we still see the number of outliers that fall beyond the allowable range through the numbers at the ends of the boxplots, but we do not see their actual locations.

Figure 4(a) shows the distribution of the z-transformed correlation coefficients when the underlying data is simulated, Normal (0,1). At each subsample size, the mean and standard deviation are close to the theoretical n^{-1} and $n^{-1/2}$ respectively. The skewness and kurtosis at subsample size n_1 = 10 are far from the theoretical Normal distribution values of 0 and 0, reflecting partly the one far outlier at -3.8 and partly the negative skew in the remainder of the n_1 is. For other subsample sizes, there is no strong evidence to contradict the assumption of approximate Normality.

The relationship between Figure 4(b) and 4(a) is similar to that between 3(b) and 3(a). Figure 4(b), which is based on simulated χ^2_1 data, shows (a) bias that is the same as for the transformed correlations based on Normal data, (b) slightly



suppressed variances, particularly at small subsample sizes and (c) positive skewness which persists at large subsample sizes. In addition, there are signs of positive kurtosis at small subsample sizes.

Figure 4(c) is based on Lognormal (0,1) data and shows high values of skewness and kurtosis at almost all subsample sizes. Approximate Normality seems an unwarranted assumption. In fact, the kurtosis is converging very slowly to its asymptotic value of 0.

In general, using the z-transform does not help with Normality assumptions, especially when dealing with long-tailed distributions.

F. SIMTBl OUTPUT FOR THE 2-FOLD JACKKNIFE OF THE CORRELATION The final Figures, 5(a), 5(b) and 5(c), deal with the 2-fold jackknife estimate of correlation. Again, the figures are reduced graphics with scaling comparable to that of the boxplots of Sections VI.D and VI.E. To define the estimator, we start with a given subsample of size n, compute the serial correlation for the first $\lfloor n/2 \rfloor$ points and call it $r_1(n/2)$, compute the serial correlation for the second $\lfloor n/2 \rfloor$ points and call it $r_2(n/2)$ and compute the serial correlation for the entire subsample of n points and call it $r_0(n)$. Each computation follows the formula in Section VI.B. The three estimators are then combined to form two pseudo-values,

$$r_1*(n) = 2r_0(n) - r_1(n/2)$$



and

$$r_2^*(n) = 2r_0(n) - r_2(n/2)$$
,

and the final jackknife estimator for that subsample is defined as

$$\tilde{r}(n) = \frac{r_1^{*n} + r_2^{*(n)}}{2}$$
.

Although a jackknife estimator may have many favorable properties, we are concerned here primarily with its ability to remove bias, hopefully without inflating the variances of the estimator and/or inducing nonnormality.

Figure 3(a), based on simulated Normal (0,1) data, shows nearly complete removal of bias, even at small subsample sizes. The cost of the bias reduction is reflected in an increase of nearly 50% in the standard deviation of the correlation estimate for subsample size 10, and lesser relative increases at larger subsample sizes. There is also an indication of a positive skew for small subsample sizes, and the problem that the jackknife estimator need not fall into the -1 to +1 range which is desirable for a correlation coefficient estimate.

When using simulated χ^2_1 data as in Figure 5(b), or simulated Lognormal (0,1) data as in Figure 5(c), there is again no problem with bias. Variance inflation, though it exists



at small subsample sizes, is not as large as when Normal (0,1) data is used. The distributions of the jackknifed correlations show very pronounced positive skews, however, as well as positive kurtosis. These two problems are worse for the longer-tailed Lognormal data.

Overall, the jackknife estimator is very successful at removing bias but the costs include variance inflation, which can be severe at small subsample sizes, plus increased positive skewness and kurtosis when the estimates are based on data from longer-tailed distributions.

G. COMPARISON OF THE THREE ESTIMATES OF CORRELATION

For Normal (0,1) data, the distribution of the usual correlation coefficient displayed in Figure 3(a) behaves very much as theoretical asymptotic calculations would predict, even at small subsample sizes. This makes it possible to correct for bias in the estimator and to perform tests of significance. Use of Fisher's z-transform, as illustrated in Figure 4(a) does not seem necessary since it does not significantly improve the approximate Normality of the estimator. The jackknife estimator in Figure 5(a) may be valuable if a direct, unbiased estimator is needed but the inflated variance of the jackknife estimator may limit the usefulness of the estimate as well as make any tests of significance too conservative.

When the underlying data comes from a longer-tailed distribution, the usual correlation coefficient in Figures 3(b)



and 3(c) retains a predictable bias term, although the variance of its distribution is slightly depressed and the skewness and kurtosis becomes positive, even for subsamples as large as 150. This means that it is still possible to estimate the correlation accurately, but tests of significance fall on shakey assumptions of Normality. The z-transform in Figures 4(b) and 4(c) does little to firm up those assumptions and, in some cases, makes the situation worse. As in the case of Normal data, the 2-fold jackknifed correlation in Figures 5(b) and 5(c) is bias-free but follows a fairly non-Normal distribution which would invalidate significance testing.

All of the preceding observations and conclusions flow immediately from the nine figures presented so far. Further studies could easily be done through SIMTBl, looking at larger subsample sizes, correlated data, and alternative marginal distributions. For demonstration purposes, though, it is better to proceed to our second application.



VII. STUDY OF PROBLEMS OF ESTIMATING SHAPE PARAMETERS FOR HIGHLY SKEWED DISTRIBUTIONS

A. ESTIMATING THE SHAPE PARAMETER FOR A GAMMA DISTRIBUTION

As a second application of SIMTB1, we will consider a

problem which has received much less statistical attention;

asymptotic results are summarized in Cox and Lewis (1966,

Ch. 2) [Ref. 7] and Johnson and Kotz (1970, Ch. 17) [Ref.

8]. We want to estimate the shape parameter, K, for a Gamma distribution, where the Gamma density is given by

Notice that the mean of this distribution is u, not K/u as in some differently parameterized versions of the Gamma density. For the data that will be simulated for use in SIMTBl we will use K = 5 and u = 1 and K = 0.25 and μ = 1. The closer the mean of our estimate is to 5 or 0.25, the better (in terms of bias) is our estimation procedure. Other factors such as the variance and Normality of the estimator will of course also have influence in the determination of a preferred estimator.

Section VII.B will compare the commonly used maximum likelihood estimator to the competing method of moments



estimator. Both procedures result in asymptotically Normal estimators (Cramer, 1948) but the m.l.e. is usually preferred because of its favorable asymptotic relative efficiency (Cox and Lewis, 1966) [Ref. 7]. Through SIMTBl, though, we will see that for small subsamples the estimated variances of the two estimators of K are not as far apart as asymptotic results lead us to believe. In addition, the bias that appears in both estimators is smaller for the moment estimator.

In Section VII.C. we will use a four-fold jackknife of both the m.l.e. and moments estimators to successfully remove the bias. What is remarkable is that, unlike the jackknifing of the serial correlation, there is little or no cost in terms of variance inflation and nonnormality for the jackknifed moment estimator. When K = .25, we will see in Section VII.D. that the jackknifed m.l.e. dominates the other three estimators at all subsample sizes when considering the mean, variance, and Normality of the estimator.

- B. MAXIMUM LIKELIHOOD AND MOMENT ESTIMATORS OF K
- Figure 6(a) is very similar in format to the figures that have already been presented for the correlation example except that:
- (1) The estimator whose distribution is being displayed is the maximum likelihood estimator of K, the shape parameter of a Gamma(5) population. We denote the estimator, computed from a simulated subsample of size n, by $\hat{K}(n)$ and define it



to be the solution of the equation:

$$n[\log \hat{K}(n) - \Psi(\hat{K}(n))] = n \log \sum_{i=1}^{n} X_i/n - \sum_{i=1}^{n} \log X_i,$$

where the X_i are the simulated Gamma(5) random variables and $\Psi(\cdot)$ is the digamma function (Cox and Lewis, 1966).

- (2) The eight subsample sizes which we will be looking at are $n_1 = 33$, $n_2 = 50$, $n_3 = 71$, $n_4 = 100$, $n_5 = 125$, $n_6 = 166$, $n_7 = 250$ and $n_8 = 500$. We will not see as much detail at small subsample sizes but we will see some of the asymptotic (n = 500) effects coming in.
- independent replications of N* = 2500 simulated Gamma(5) random variables, instead of the M = 10 replications of N = 5000 variables used previously. The total number of independent simulated random variables across replications remain constant at the program maximum of 50,000. Hence, the boxplot at subsample size 50 in Figure 6(a) represents the distribution of M* $\left[N*/50\right]$ = 1000 estimates of $\hat{K}(50)$ just as the boxplot at subsample size 50 in Figure 3(a) represents the distribution of M* $\left[N/50\right]$ = 1000 estimates of r(n). As long as the product, M × N, remains constant, the only effect that changing the number of replications has, up to rounding in $\left[N/n_{\frac{1}{2}}\right]$, is to change the results in the regression on the averages. By using M* = 20 and N* = 2500, SIMTBl reports regression coefficients averaged over 20 replications, but,



within each replication, the dependent variables are averages over just $2500/n_{\rm i}$ values of the estimator.

(4) The boxplots are presented using the reduced graphics option. In this option any extreme outliers (i.e., those beyond 1.5 interquartile distances) are included as a count at the tail of each boxplot. This option was chosen in order to give more graphical weight to the body of the distributions and the fall-off in the bias. Limited printer resolution makes it impossible to show details in the body and the tails of the distributions if there are many straggling outliers. In the case of very extreme outliers, no detail would be seen in the body of the boxplot without the reduced graphics option.

Figure 6(b) looks at the distribution of the moment estimator of K, the shape parameter of a Gamma (K) population:

$$\widetilde{K}(n) = (n-1) \overline{X}^2 / \sum_{i=1}^{n} (X_i - \overline{X})^2$$

where $\overline{X} = \sum_{i=1}^{n} X_i/n$, n is the subsample size, and the X_i are the simulated Gamma(5) random variables. The SIMTB1 options and parameters mentioned in (2), (3) and (4) preceding are also in effect here.

The two Figures, 6(a) and 6(b), show a very pronounced bias in both estimation procedures, although the moment estimator is slightly closer to the unbiased value of 5.

As expected, the standard deviation of the m.l.e. is lower than that of the moment estimator although the relative



difference at small subsample sizes, for instance 1.448 versus 1.482 at $n_1=33$, may not outweight the increase in bias with the m.l.e. At larger subsample sizes, the relative difference is close to the theoretical asymptotic relative efficiency of .78 (i.e., .91 at $n_7=250$).

Both estimators also show distributions with positive skewness and kurtosis that decrease to the asymptotic 0 levels as subsample size increases. The asymptotics appear to take hold more quickly for the moment estimator than for the m.l.e.

In summary, SIMTBl shows that the m.l.e. is indeed better than the moment estimator in terms of variance, but not as good for small sample sizes as asymptotic results would lead us to believe. In the other areas of bias and asymptotic Normality, the moment estimator would have to be preferred.

C. 4-FOLD JACKKNIFED ESTIMATORS OF K

Figures 6(c) and 6(d) show the distributions of the 4-fold jackknife m.l.e. of K and 4-fold jackknifed moment estimator of K, respectively. A 4-fold jackknife estimator is similar to the 2-fold jackknife estimator described in Section VI.F. except that there are 4 pseudo-values that come out of dividing each subsample into fourths. More details can be found in Mosteller and Tukey (1977) [Ref. 6].

The purpose of the jackknife is to remove the conspicuous bias observed in Figures 6(a) and 6(b). This goal is seen to be accomplished in Figure 6(c) and 6(d) and we can also note



smaller values of skewness and kurtosis, indicating a quicker approach to asymptotic Normality. The skewness and kurtosis of the jackknifed moment estimator are the lowest, at small subsample sizes, among all estimators. The variance of the jackknifed moment estimator is also only slightly inflated, as is the variance of the jackknifed m.l.e.

All told, the jackknifed moment estimator, because of its lack of bias, small variance, and low skewness and kurtosis, would be the method of choice if estimation of K or significance testing was the goal.

D. RESULTS FOR K = 0.25

In Figures 7(a), 7(b), 7(c) and 7(d) we show similar results to those discussed above for the case K = 5.0, but using K = 0.25. The fact (Cox and Lewis, 1966, Ch. 3) [Ref. 7] that the m.l.e. estimate is much more efficient than the moment estimate is graphically illustrated. What is new is the effect of jackknifing: bias is reduced without the sacrifice of variance inflation or nonnormality.

Further comparisons and interpretations are similar to those done for the case K = 5.0, and are left to the reader.

E. CONCLUSIONS

Simply by providing SIMTBl with the desired estimators, we have been able (a) to explore in depth the effects of changes in data distribution and of different estimation procedures on the calculation of the serial correlation



coefficient, and (b) to compare four different ways to estimate the shape parameter in a highly skewed Gamma population.

The graphics and numerical output combine to let us see and quantify distributional changes that occur as subsample size grows. We can see bias fall away, variance shrink, and skewness disappear as the estimator approaches asymptotic Normality. Terms in the asymptotic expansion of the mean and variance of the estimator are automatically calculated and can be used to compare different estimators.



VIII. COMPARISON OF DIFFERENT METHODS FOR ESTIMATING THE VARIABILITY OF THE STANDARD DEVIATION OF CORRELATION ESTIMATES

A. INTRODUCTION

Bradley Efron and Gail Gong (1982) review in their article, "A Leisurely Look at the Bootstrap, the Jackknife, and Cross-Validation" [Ref. 9] different methods for estimating statistical error of parameter estimates. They discuss in particular the problem of estimating the error of a statistical estimator with the example of the estimates of the standard error for the correlation coefficient of a bivariate normal distribution. They compared the standard deviation estimates of different methods using 200 simulations at one fixed sample size of 14.

SIMTB2 was used to explore the distributions of the estimates they used in their article. The bootstrap, the jackknife, the infinitesimal jackknife (delta method) and the normal theory are the methods for which the distributions were explored. The estimation methods will not be explained in detail (see Efron and Gong in The American Statistician, Feb. 1983, Vol. 37, No. 1), only the setup of SIMTB2 and the output will be discussed.

B. SETUP OF SIMTB2 AND THE ESTIMATOR FUNCTIONS

The bivariate normal distributed input data with known correlation 0.5 was generated with an IMSL random number



generator (GGNSM). 14,000 bivariate data points were generated and then sectioned into 10 blocks, each having 1,400 points (M = 10, N = 1400). The subsample sizes (NE(k)) used are 10, 14, 20, 28, 35, 40, 70 and 100. Only subsample size 14 was used by Efron and Gong.

The program had to be run with 5 different standard deviation estimator functions. SIMTB2, as the other versions, can only handle up to 3 estimator functions in one program run. To make the given outputs comparable the fixed scale option (SVS = 1, YMIN = 0.0 and YMAX = 0.7) was chosen.

The bootstrap estimate of standard deviation was done with 2 different numbers of bootstrap replications (B = 128, B = 512). So for the subsample size of 14, the bootstrap procedure with B bootstrap replications in itself was done (1400/14 = 100; 100*10 = 1000) 1,000 times.

The jackknife function followed the standard jackknife procedure and used the jackknife formula for the standard deviation:

$$S_{jack} = \left[\frac{n-1}{n} \int_{i=1}^{n} (\overline{X}_{(i)} - \overline{X}_{(\cdot)})^{2}\right]^{1/2}$$

with

$$\hat{\Theta}_{(j)} = \hat{\Theta}(x_1, x_2, \dots, x_{i-1}, x_{i+1}, \dots, x_n) \quad \text{for } \overline{X}_{(i)}$$

and



$$\hat{\Theta}_{(\cdot)} = \frac{1}{n} \sum_{i=1}^{n} \hat{\Theta}_{(i)}$$
 for $\overline{X}_{(\cdot)}$

The delta method (infinitesimal jackknife) function calculated the estimate with the formula:

$$\mathbf{S_{Delta}} = \{ \frac{\hat{\rho}^2}{4n} [\frac{\hat{\mu}_{40}}{\hat{\mu}_{20}^2} + \frac{\hat{\mu}_{04}}{\hat{\mu}_{02}^2} + \frac{2\hat{\mu}_{22}}{\hat{\mu}_{20}\hat{\mu}_{02}} + \frac{4\hat{\mu}_{22}}{\hat{\mu}_{20}\hat{\mu}_{02}} - \frac{4\hat{\mu}_{31}}{\hat{\mu}_{11}\hat{\mu}_{02}} - \frac{4\hat{\mu}_{13}}{\hat{\mu}_{11}\hat{\mu}_{02}}] \}^{1/2}$$

with

$$\hat{\mu}_{gh} = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \overline{Y})^g (Z_i - \overline{Z})^h$$

and

$$X_i = (Y_i, Z_i)$$

In doing the actual calculations for the delta method, for small subsample sizes (10,14,...,40) the value of the variance becomes negative. A negative variance can not be interpreted with much meaning. The number of negative values goes down (from 305 for NE(1) = 10 to 18 for NE(6) = 40) with increasing subsample size. Most of the negative values are small. To solve the programming problem (square root of a negative number) the function sets this negative value to 0.0D0.

For the normal theory estimate, instead of carrying out a bootstrap, an approximation formula was used. It is the



same formula the article uses for the comparison.

$$S_{norm} = \frac{(1 - \hat{\rho}^2)}{\sqrt{(n-3)}}$$

See Efron and Gong for details.

C. INTERPRETING THE SIMTB2 OUTPUT

The output of the program runs is provided as Figures 6, 7, 8, 9 and 10. A comparison of the numerical output (subsample size 14) with the results is done in Table 3.

The bootstrap procedure (Figures 8 and 9) was done with 2 different numbers of bootstrap replications (B = 128 and B = 512). Both distributions for the standard deviation (S.D.) look very similar. Both are positively skewed with some outliers at the right tail. In both cases the outliers are in the same range. As the boxplots and the summary statistics show, the increase of the number of bootstrap replications (B) does not result in a large improvement in the performance of the estimation function.

The jackknife estimate (Figure 10) has a positively skewed distribution with outliers. The distribution of the jack-knife estimate looks very similar to the distribution of the bootstrap estimates. For small subsample sizes the bootstrap distribution has more outliers. Overall the performance of the jackknife procedure is as good as the bootstrap, but the jackknife needs less computer time.



ESTIMATES OF THE STANDARD DEVIATION FOR THE CORRELATION COEFFICIENT FOR A BIVARIATE NORMAL WITH TRUE CORRELATION p = .5

* negative values set to 0.0



The distribution of the estimates produced by the delta method (Figure 11) is negatively skewed and has nearly no outliers. But in calculating the estimates the problem of negative values for the variance came up. For some subsamples, the final estimate (the standard deviation) could not be calculated, since the corresponding value of the variance was negative. In these cases, the standard deviation was set to 0.0. This procedure influences the distribution and the summary statistics. The influence is more important for small subsample sizes than for larger ones. So the graphical and numerical output should be seen with this fact in mind.

The normal theory function (Figure 12) produces estimates with a negatively skewed distribution but only a few outliers and the distribution is tailed to the left. The tail of the distribution is in the opposite direction of all other distributions. For the estimate of the standard deviation for the correlation coefficient the result of the normal theory is close to the true result. This may not be valid for other estimators.

In addition to the comparisons Efron and Gong did, with SIMTB2 it is easy to investigate how the sample size will influence the estimate of the standard deviation of the correlation coefficient. In Table 4 the methods are compared for a subsample size of 10 and 100. With increasing subsample size the quality of the estimate should improve, but the



WITH TRUE CORRELATION SIMTB2 (M = 10, N = 1400) FOR THE CORRELATION COEFFICIENT FROM A BIVARIATE NORMAL ρ = 0.5 AT DIFFERENT SAMPLE SIZES. ESTIMATOR OF THE STANDARD DEVIATION

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1400 Trials Subsample Size 10	S.D.	0.083	0.082	0.13	, 0.12*	7 0.082	7
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		Bootstrap B = 128	Bootstrap B = 512	Jackknife	Delta Method	Normal Theory 0.027	True Value

negative values for Variance set to 0.0



improvement may be different for the different methods of estimation. By making the subsample size 10 times larger, with the SIMTB2-side effect of reducing the total number of calculated estimates, the bootstrap improves less than the jackknife, delta method and normal theory.



IX. FINAL CONCLUSIONS

SIMTBED with the different versions can be used on digital computers of different size (mainframe to micro) and type. The limitations in using the program are given more by hardware constraints like memory size and computer time than by the program itself.

The FORTRAN program is completely portable, changes in the code, may only be necessary to adapt the program to special restrictions given by a special type of hardware. This may occur in using micro computers more often than with mainframe computers. Up to now all versions of code are written for the more normal standard computer environment and do not need special equipment (color printer, etc.). Additionally hardware dependent features like color output can improve the graphics of the program.

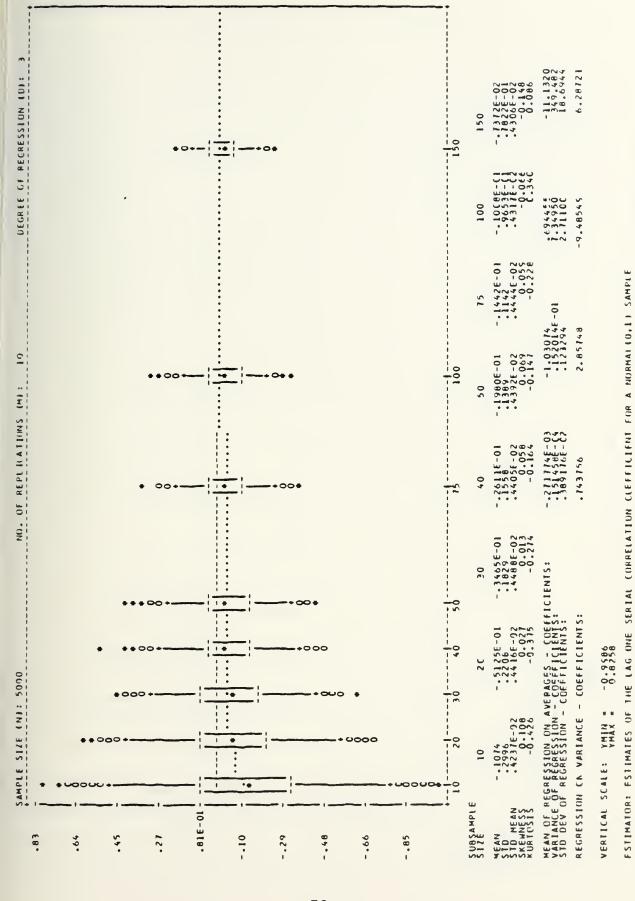
SIMTBED makes it easy to evaluate the result of statistical experiments. The combination of graphics and numerical summaries for different sample sizes make it easy to judge the distributional behavior of a statistical estimator. The result can be seen without additional computations in the graphic outputs. Comparing only the boxplots it is possible to judge the influence of subsample size on the variability of an estimator.



Besides for research the program can be used in showing students the distributional behavior of different estimators in a pictorial way. It is easy to compare the different behavior of similar estimators (e.g., biased vs. unbiased estimator of the variance) for different sample sizes.

The easy use and the fast visual impression of the distributional behavior of an estimator, given by the graphic output is one of the advantages in using SIMTBED. Besides this fast first visual impression all necessary and needed numerics are given for further and deeper investigations.





Estimates of the Lag One Serial Correlation Coefficient for a Normal (0,1) Sample Figure 3a.



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Estimates of the Lag One Serial Correlation Coefficient for a Chi-Square (1) Sample Figure 3b.



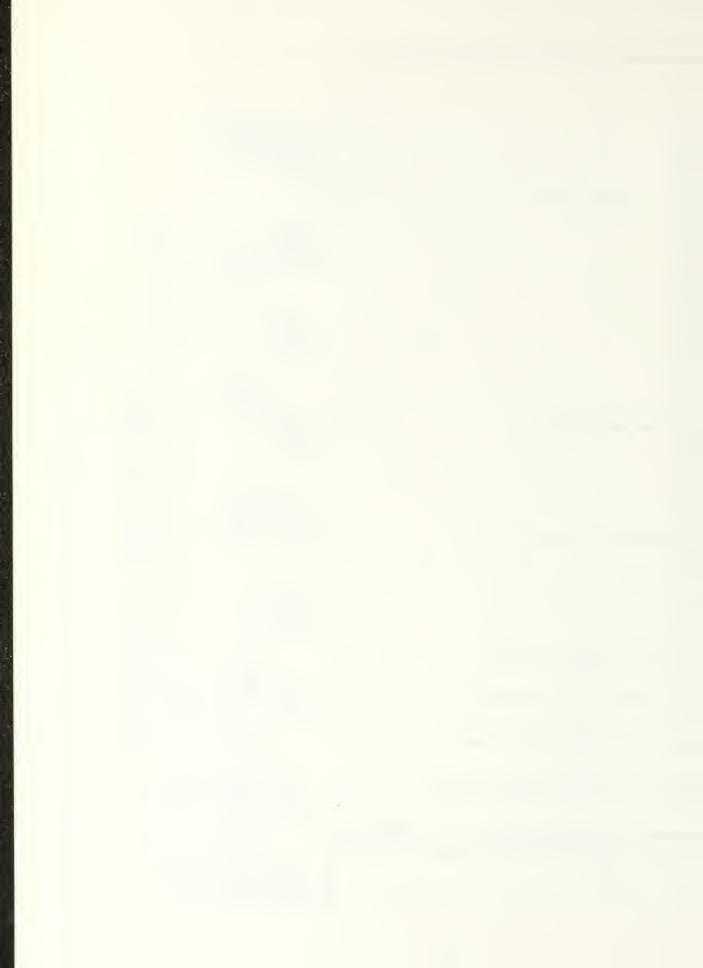
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Estimates of the Lag One Serial Correlation Coefficient for a Lognormal (0,1) Sample Figure 3c.



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Coefficient for a Normal (0,1) Sample



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Estimates of the Z-Transform of the Serial Correlation Coefficient for a Chi-Square (1) Sample Figure 4b.



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Estimates of the Z-Transform of the Serial Correlation Coefficient for a Lognormal (0,1) Sample Figure 4c.

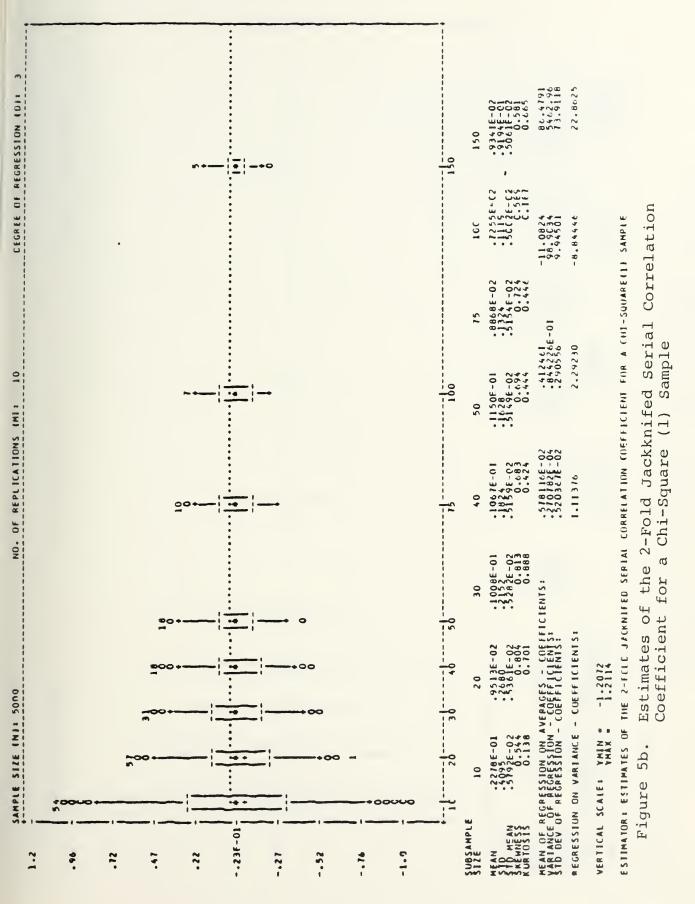
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Coefficient for a Normal (0,1) Sample









the Shape Parameter 5.0) ESTIMATCE: MAXIMUM LIKELIHOOD ESTIMATE OF THE SHAPE PARAMETER OF THE GAMMA DISTRIBUTION K=5. of of the Gamma Distribution (k = Maximum Likelihood Estimate Figure 6a.



FEGFESSION (D):	00		\$10 4 cq7 3 750 - 3 750F-C1 - 0.482 - 0.135	4202,59 9491176,01 3145,01 -3740,92	
DEGREE CF			250 5.028 .3726 0.356	-196.572 23214.0 152.361 2162.90	
			5.054 .6277 .36247 -0.184	97~ 7 200	
S (M): 2C			125 5.080 .7313 .2747E-01 0.525 0.373	15,434 4.1480 2.0366 -336.83	
OF REPUBLICATIONS		250	100 5.113 .8241 .3705 0.375	4. 56.799 .9662836-03 .3169516-03 81.7175	
no.	moo o	166	71 5-151 -9606 -2631E-01 0-670	FICIENTS:	
2500	-000+	100 125	5.234 1.177 1.3721E-C1 1.065	COEFFICIENTS: COEFFICIENTS: COEFFICIENTS:	1.0544
PPLE SIZE INTE		33 56 71	5.371 1.482 1.627E-C1 1.512	GRESSIEN CN ZVI F REGRESSIEN - C REGRESSION - C ON VARIANCE -	SCALE: YPIN
4 I		3 4 0	TANATA 100	VARIANCE OF P VARIANCE OF P STE CEV CF RI PESRESSICN OF	VERTICAL SO

ESTIMATOR: MOMENT ESTIMATOR (RECIPROCAL " SCHARFO CHEFFICIENT OF VAPIATION) OF THE SMAPE FADAMETER OF GAMMA DISTRIBUTION K=5. Figure 6b. Moment Estimator (Reciprocal of Squared Coefficient of Variation) of the Shape Parameter of the Gamma Distribution (k = 5.0)



REGPESSIEN (0): 3		ပ	500 5.031 .6846 .6846 0.465 -0.446	-7111.72 .037448E.05 30/17.6
DEGREE OF REGR			250 4.968 7210 50986-01 -0.045	249.841 .25729E+C1 1604.0E 87628.4
			5.010 .7624 .4402F-01 -0.364	ann a
			12 % 5.008 .4259F-01 0.361	-7-1772 550-28 24-295 -11703-
A STATE OF THE STA		250	4.577 4.577 .9542 .42675-01 0.230	5. C2893 -103702F-01 -101624 587-234
	mana	•	71 4.570 1.912 . 38265-01 1.765	ICIENTS:
	***************************************	}	10000000000000000000000000000000000000	VERRGES - CCEFFI CCEFFICIENTS: CCEFFICIENTS:
		1 11 35 8	4 - 517 1 - 5 5 5 6 - C1 2 5 2 5 6 - C1 2 - 6 4 0	SECRESSION - CECEESSION - CECEE
1.0	2 2 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	SUESAMFLE	A DE LE	PEAN CF FEGP VARIANCE UF FEGE CF PECP

ESTIMATOR: 4-FOLD JACKNIFEC MAXIMUM LIKELIFORD ESTIMATE OF THE SAMMA FISTRIBUTION KES.

Figure 6c. 4-Fold Jackknifed Maximum Likelihood Estimate of the Shape
Parameter of the Gamma Distribution (k = 5.0) YMAN . 9.13:2

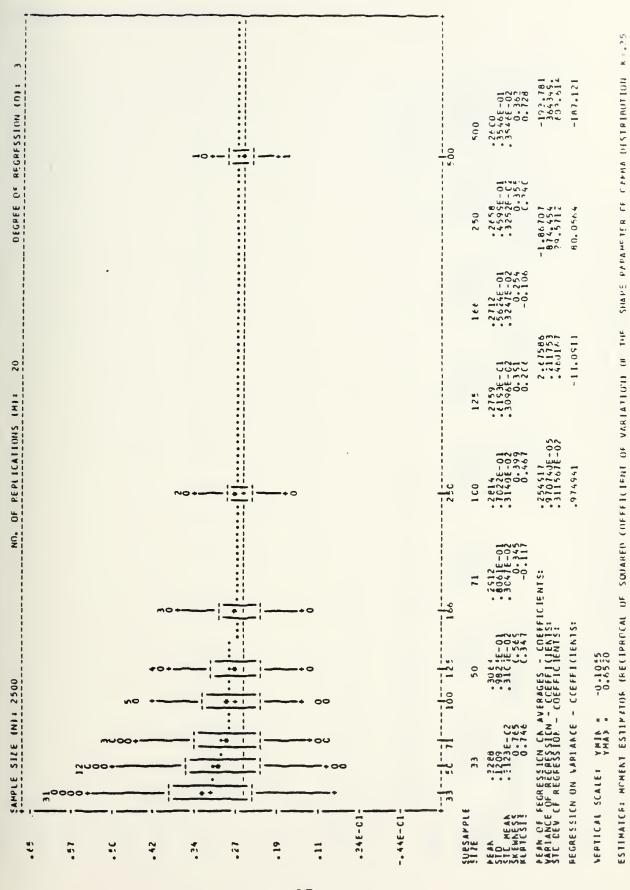


SAMPLE SIZE	- N	2500	NO.	OF REPLICATIONS	S (M): 2C		DEGREE CF RE	REGFESSION (CIT 3
2 4 5 5 6 6 4 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		5000						
SUPSAMPLE S126		50	11	100	125	164	250	200
2000 2000 2000 2000 2000 2000 2000	36-01 -651 -6691	4.951 1.21 1.21 1.385:E-01 (.464	4.958 . \$655 . 3725E-01 0.738	4.984 . 2476 . 375 201 0.517	4.977 • 7416 • 2768F-C1 0.515	4.5E0 .6342 .7662E-01 -0.437	4. 575 . 5298 . 37466-61 0.325	4,565 -3734 -27346-01 -0.461
MEAN OF REGRESSION VARIANCE OF REGRESSION ON VARI	SIEN - C	- CCEFFICIENTS: - CCEFFICIENTS: - CCEFFICIENTS:	ICIENTS:	4.96213 .965102E-03 .301513E-01	5 41940 13 9244 3 7 15 2 - 3 8 2 3 3 2		91680.1 91680.1 303.117 3397.67	6531.21 -7671.08 -7671.09
VERTICAL SCALES Y	Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y	1.0544						
ESTIPATORS 4-FOLD	CKN IF	EC MOMINI EST	ICR OF 1	MOMONE TO	THE GAMMA	ISTRIBIJI + H	2	
Figure	oa.	4-roid Ja Paramete	ackknired r of the (Moment Es Samma Dist	nmator o ibution	(k = 5.0)	ipe ipe	



PFE UF REGRESSION IC):	0	250 250 - 1925 - 1821 - 1821 - 193 - 1
0£ G PF E		F=-01 F=-02 F-03 F-05 F-170 F-
F REPLICATIONS (M): 20		124 -25956-01 -25956-02 -12996-02 -448 005 -663 -663 -663 -663 -663 -663 -663 -663
110. (1F		9 5
SAMPLE SIZE (N): 2500	MO+	SUBSAMPLE 33 50 71 10C 12: 50 12





Variation) Of Moment Estimator (Reciprocal of Squared Coefficient of the Shape Parameter of the Gamma Distribution (k Figure 7b.



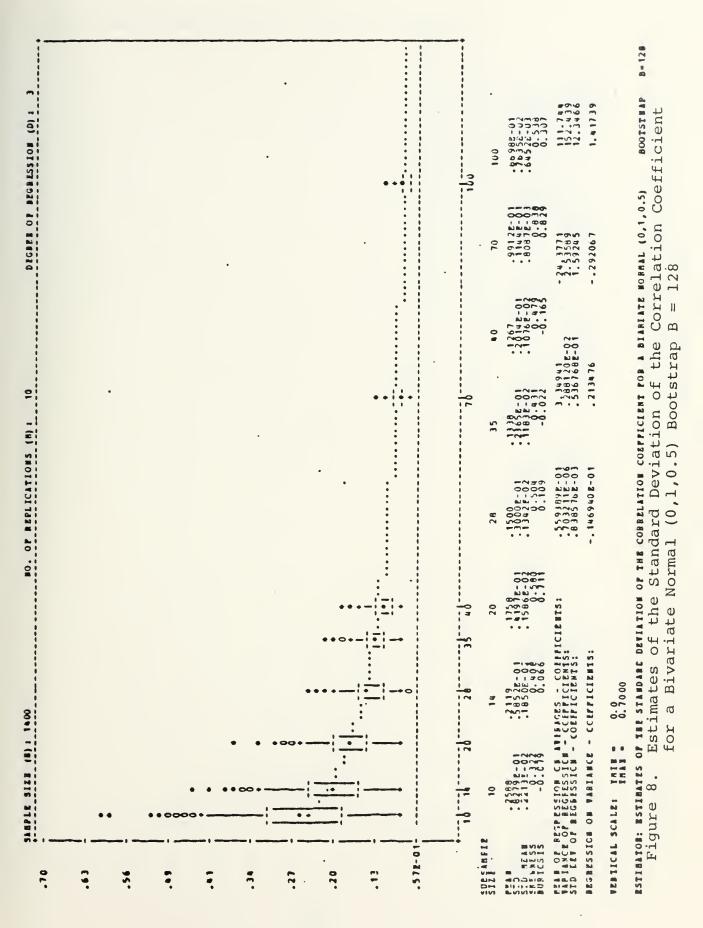
11	- 63.	 	 		61.	-+0	.24E-01-	44E-C1-	33	SUPSAFEE 3	KINIMA KANAMA KA	JARIANCE OF RECRE	FEGRESSICH ON VI
11			1444	:					15-	G1 P1	131756 131756 10.996 10.996	S S S S S S S S S S S S S S S S S S S	LARIANCE -
711 100 0 12:			.		•					50	25 415 1915 1915 1915 1915 1915 1915 1915	₩ ∀) ••	VI
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125 125 126 127 128 128 128 128 128 128 128 128					-+ U				250	100	2516 2809 1256 0	52554 08554E-0 44414E-0	38654F
166 250 500										~	2520 25155- C 1787E- C 0.43	(2450 18109 13457	24163
250 250 250 250 300 252 -128 x = -01 181 x		•		•					0 0 0 0 0 0 0 0 0 0 0	40	2523 2250E 1322E 00.	SE -01	-
5 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0										250	2523 18186~0 129 46-0 - C-17	16.478 16.478 0.7525	12:1.2
				0+	•					205	257	C . A	. 0533

AICE! 4-FCLO JACKNIFEE PAXIMUP LIKELIFGOD ESTIMATE OF THE SHAPE PARAMETER OF THE GAMMA PISTRIRUTION ---25 4-Fold Jackknifed Maximum Likelihood Estimate of the Shape Parameter of the Gamma Distribution (k = 0.25) Figure 7c.

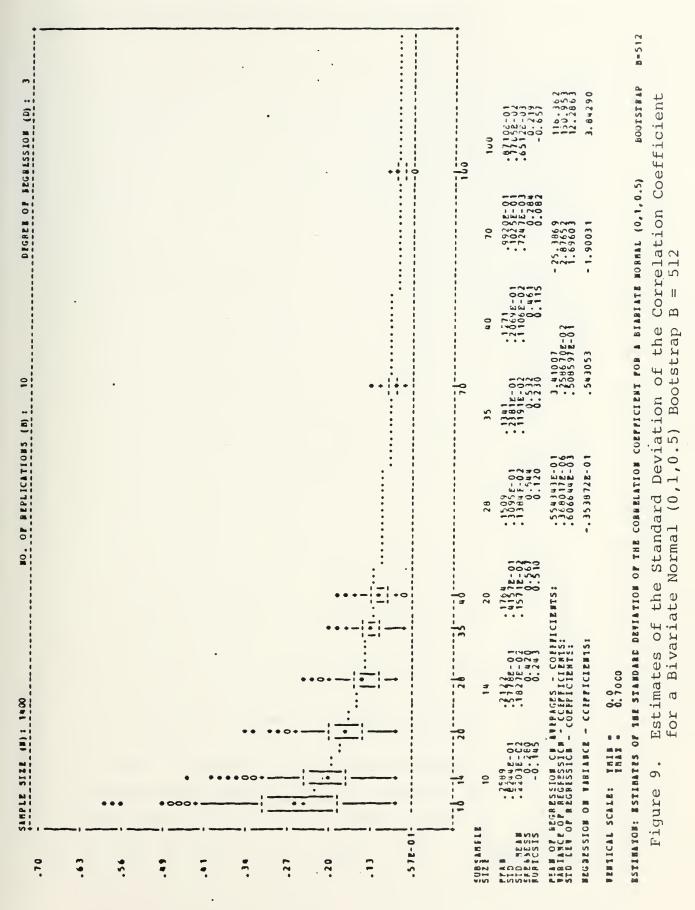


SAMPLE	E S12E (N):	2500	NO.	OF REPLICATIONS	(H): 20		DECAFF OF PF	GRESSION (D): 3	
24 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 +	00000	**************************************							•
- 66	16 36	160 125 11	991	250	• E E E E E E E E E E E E E E E E E E E	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		000	•
SLESAPFIE S17E	E1	20	11	100	125	166	250	500	
TINITE PARTICIONISTE PARTICION	. 4115E-C2 -4115E-C2 -0.158	262; -122; -388;E-C2 -C154	. \$6.79 . \$6.79 . \$6.58 . \$6.50 . \$0.20 . \$0.45 . \$0.45	.2561 .8482E-01 .3793F-02 -0.136	.7370E-01 .3685E-02 -0.163	.2549 .6441E-01 .3731E-02 -0.153	. \$609.2E - 01 . \$609.2E - 02 . \$60.1E - 02 . \$60.171	. 2541 . 37734 - 01 . 37734 - 02 -0.014 1.329	
VERNOCE FEGRESTIC OF RESTRESTICEN CF WE	CEESSICN CA PROPERTY OF THE PR	COEFFICIENTS: COEFFICIENTS: CCEFFICIENTS:	FICIENTS:	.255242 .146565E-04 .362838E-02	-, 374536 -, 493583 -, 695401 -1,48800		53.4121 3064.30 65.3561 4.12576	-877,151 153388F+07 1234,46 42,2454	
VERTICAL SCALE	E: YPIP =	-0.1055							
ESIIMATCR: 4-FC Figure	7d.	Jackiffer wingful Esti d. 4-Fold Jac Parameter	r estrance of the sales danker of the Gam	Moment Estimator of the Bhape amma Distribution (k = 0.25)	Estimator of the stribution (k =	he Shape = 0.25)	K = +25		

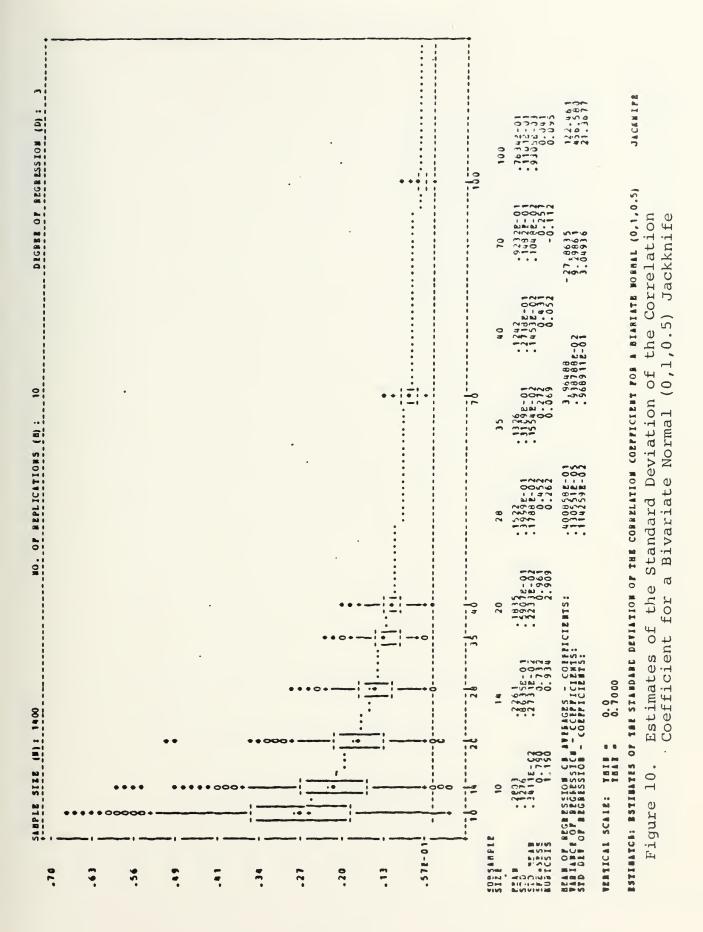




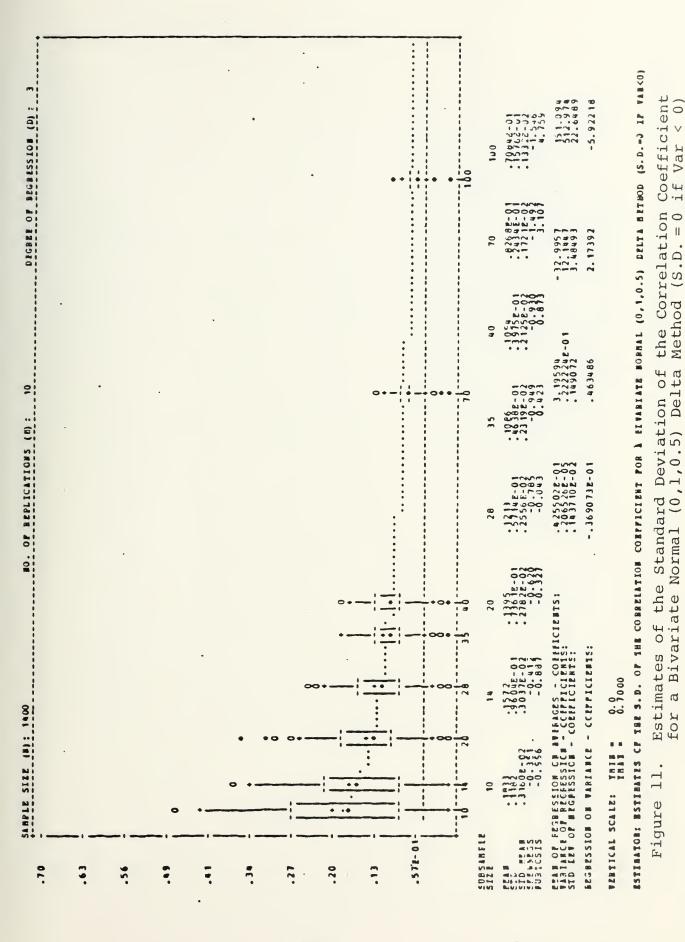
















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Ē Z REGRESSIONS. NOT IARGE E REGRESSIONS. ⊕ 0 • EL FRODUCE 2 ō S12 E US. G, × 000 ഗ NI 0 田田 N SE шŴ SAMPLE SIZ TO LARGES FER THAN N AMPL STORED 50, œ WILL m SO EXCEED ISEXC KILL NCE NORI TH AT AN AND VARIAN F THE SAMPIE D=O WILL IGN TATI m z THAT OF SIZE & CONTAINING SUBNE MUST BE FROM SMALLESS THE ARRAY NE CAN BE GREGUST NOT EXCEED 12,500. z Ž CAR NOT NE (8) CTION DATA. DATA. S EPLICATIONS) ND M*N MUST BOXPLOT ũΖ SIZES FROM MEAN E IF 1 S# ER D EXCEED 50,000 ANI N FOR NTAINING 1 OF A A ER SSION ED B SECTIONS EXCEED 100 SUBSAMPLE NUMB 500 GRES THE > 12 12 12 X TEGER ARRAY

F VALUES OF

ELEMENT OF

(N/NE(1)) M RAY OF 田田田 M E •0 CANNOT 1 E L * 4 AR N S 百百日 CANNOT MEER OF 08 EGREE WILL NCUGH. ZEO# D ZZ HEGH GL) CA ZI HHZE 90E (±) E z 0 × z

S GEAPHS L TO 15 AT TIMES WER ш SCALING ***
SCALING IS ACCOMPLISHED BY TAKING THE SMAILEST AND THE
IARGEST ESTIMATE VALUES FROM ALL ESTIMATING FUNCTIONS
AND FROM FOF ALL SUBSAMPLE SIZES.
THE SEI PARAMETER ALLOWS THE USER TO SCALE THE GFAPE
CF EACH ESTIMATOR INDIVIDUALLY OR TO SCALE THEM ALL TO
THE SAME SCALE.
SCALE SCALING ALL TO THE SAME SCALE IS
ACCOMPLISHED BY TAKING THE MINIMUM AND MAXIMUM ESTIMAFROM ALL THE ESTIMATORS USING NE (1) SUBSAMPLE SIZE.
THE RG FARAMETER ALLOWS THE USER TO RREDUCE THE VER
TICAL SCALE TO: THE UPPER QUARTILE LISTANCE + 1.5 TIME
INTERQUARTILE DISTANCE AS THE MAX VALUE AND THE LOWER *

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CUARTILE - 1.5 TIMES THE INTERQUARTILE DISTANCE AS THE AIN VALUE. THE INTERQUARTILE DISTANCE IS COMEUTED FROM THE SAMPLE OF ESTIMATES FROM THE NE (1) SUBSAMFLE SIZE. IF THERE ARE NO ESTIMATES OUTSIDE THESE MIN AND MAX VALUE THERE ARE ESTIMATES OUTSIDE THESE LIMITS THEN THEY ARE COUNTED AND THE NUMBER PRINTED AT THE ENDS OF THE EX PLOTS. THE SVS PARAMET ALLOWS THE USER TO SET THE VERTICAL SCALE. WHEN THE VERTICAL SCALE IS SET THE SEI FARAMETER IS IGNORED AND THE VERTICAL SCALE BECCMES YMIN AND YMAX.	RG=0 DO NOT REDUCE THE VERTICAL SCALE OF THE GRAPHS. RG=1 REDUCE GRAPHICS VERTICAL SCALE TC UPPER (LOWER) QUARTILE + (-) INTERQUARTILE LISTANCE.	SEI=0 DO NOT SCALE ESTIMATORS' GRAFHS INDIVIDUALLY. SEI=1 SCALE ESTIMATORS' GRAPHS INDIVIDUALLY.	SVS=0 PROGRAM WILL CALCULATE VERTICAL SCALE. SVS=1 USER SETS VERTICAL SCALE TO YMIN AND YMAX.	IN LOW VALUE OF VERTICAL SCALE. SET BY USER WHEN SVS=1	AX HIGH VALUE OF VERTICAL SCALE. SET PY USER WHEN SVS=1	ST NUMBER OF ESTIMATORS THAT WILL BE USED TO CALCULATE STATISTICAL PARAMETER FROM X DATA. NEST MUST BE 1,2 OR 3.	CAICULATE THE ESTIMATOR FUNCTIONS THAT WILL EE USED TO CAICULATE THE STATISTICAL PARAMETER. CAIL SEQUENCE ON EACH FUNCTION IS: CALL FNAME(X,N) WHERE X IS THE DATA ARRAY AND N IS THE NUMBER OF DATA POINTS. THEY MUST BE DECLARED IN THE CALLING FRCGRAM (RAGE) IN THE ORDER THEY ARE USED. DUMMY VARIABLES MUST BE INSERTED WHEN THERE ARE LESS THAN 3 ESTIMATORS.	TITLES ASSOCIATED WITH EACH ESTIMATOR (EST123). A MAX OF 120 CHARACTERS CAN BE USED TO DESCRIEE EACH ESTIMATOR. EACH TITLE MUST BE DECLARED AS REAL*8 (15) ARRAYS UNLESS PASSED AS AN ARGUMENT OF THE CALLING FREGRAM RAGE. WHEN PASSING THE TITLE AS AN ARGUMENT THERE MUST BE A MINIMUM OF 120 CHARACTERS BETWEEN APOSTROPHES.	*** * * * * * * * * * * * * * * * * * *
	R G	SEI	SVS	YMI	YEA	NES	전 마 아 아 다 다 는 다 는	HHH HHH HHH	* * *



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ESTIMATORS TO THE SAME SCALE OF ESTIMATOR W/WIDEST PTS
NE, L, D, RG, SEI, SVS, YMIN, YMAX, NEST, EST 1,
SUBROUTINE SIMTB1 (X, N, I TIL1, EST2 TIL2 EST3, TT1 REAL X (50 0 CC) ULH (4), Y REAL *8 TTL1 (15), TTL2 (15) INTEGER NE (8), RG, SEI S'INTEGER D, I, NEST, TEST
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                                                                                                                                              64
                                                                                                                                               ×
                                                                                                                                                            Y KP, YMAK, YMIN)
Y KP, YMAK, YMIN)
Y KP, YMAX, YMIN)
(2) = YMIN
(4) = YMAX
ZZ
                                                                                                                                                 .
                                                                               ESTIMATOR.
                                                                             FIND VERTICAL SCALE FCR 2ND ESTIMATOR.

IF(NEST IT 2) GO TO 10

CALL SECEST(X N M NE(IK) EST2 Y KP)

IF(RG.EQ.1) CALL DELETO(Y KP, YMAK, YMIN

IF(RMIN IT ULH (2)) ULH (2) = YMAX, YMIN

IF(YMIN IT ULH (2)) ULH (4) = YMAX
                                                                                                                                             3RD ESTIMATOR
                                                                                                                                                                                                             CALLER
                                                                                                                                            FIND VERTICAL SCALE FOR 3RD IF (NEST 1113) GO TO 10 CALL SECEST(X N M NE(IK) ES IF (RG.EQ.1) CALL BELETO(Y, K IF (RG.NE.1) CALL MAXMIN (Y, K IF (YMAX GT. ULH (2)) ULH (2) ULH (4) ULH (4) ULH (4) XMIN CALCULATED SCALE TO CYMIN ULH (4)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 AT (1X, 'ESTIMATOR: '15A8)

AT (1X, 'VERTICAL SCALE: YMIN = 'F10.4,//16X, YMAX = 'F10.4,///

AT (*** ERROR... MUST BE AN INTEGER EFTWEEN 1 AND 100.

AT (*** ERROR... M*N EXCEEDS 50,000. ****)

AT (*** ERROR... M*N EXCEEDS 50,000. ****)

AT (*** ERROR... NET MUST BE 3 OR LESS. ****)

AT (*** ERROR... NET MUST BE 1 OR GREATER TO COMPUTION OR ECUAL TO 3. ***

AT (*** ERROR... M*(N/NE(1)) MUST NOT EXCEED 12 500. ***

AT (*** WARN ING... M*(N/NE(1)) MUST NOT EXCEED 12 500. ***

INCREASING SIZE. IF NE(1) IS NOT SMALLEST ELEMENT, SC.

MAY CAUSE PCINTS TO FALL OUTSIDE RANGE CF SCALE.')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             EH
                                                                                                                                                                                                                                                                                    GRA
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   QN
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   K
                                                                                                                                                                                                                                                                           FIND VERTICAL SCALE FOR 2ND ESTIMATOR A CALL SECEST (X N M NE 1), EST2 Y KP)
IF (RG.EQ.1) CALL BELETO (Y, KP, YMAX, YMIN)
IF (RG.NE.1) CALL HAXMIN (Y, KP, YMAX, YMIN)
UIH(4) = YMAX
CALL PRST (X N M EST2 NE L, RG, D, ULH, Y)
WRITE (6, 101) TIL2
IF (NEST. LT. 3) GO TO 80
                                                                                                                                                                                                                                                                                                                                         MIN
                              ZZ
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X N M EST3 NE, L, RG, D, ULH, Y)
2) TTL3
CALL SECEST (X N M NE (1), EST 1, Y KP)

IF (RG. EQ. 1) CALL MELETO (Y, KP, YMAX, YP)

IF (RG. NE. 1) CALL MAXMIN (Y, KP, YMAX, YP)

UIH (2) = YMIN

UIH (4) = YMAX

CALL PEST (X N M EST 1 NE L RG, D, ULH, N M EITE (6, 102)

IF (N EST 1 . IT. 2) GC TC 80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          KK
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FIND VERTICAL SCALE FOR 3RD E
CALL SECEST (X NA NE (1) EST3
IF (RG . EQ . 1) CALL ELETO (Y, KP,
UIH (2) = YMIN
UIH (4) = YMA X
CALL PRST (X N M EST3 NE L, RG,
WRITE (6, 101) TIL (1) ULH (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        PECERANA
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                                                                                                     NO. OF EEPLICATIONS (MUST BE <= 100)

NUMBER CF VALUES IN EACH REPLICATION (M*N MUST BE <= 50000)
USERS VECTOR WITH M CONSECUTIVE BATCHES OF N VALUES EACH
NO. OF SECTION SIZES (MUST BE BETWEEN 1 AND 8)

A RRAY WITH THE L SUBSAMPLE SIZES (MUST BE IN ASCENDING CRD
DEGREE OF THE REGRESSION (MUST BE <= 3 & <= L-1)

**XMIN, XMIN, XMAX, YMAX IN USER UNITS
ONLY UIH(2) AND ULH(4) NEED TO BE PASSED. CTHERS CALC. HER
                                      PUNCTIO
                 SUEROUTINE FRST(X N, M, EST, NE, I, RG, UD, ULH, Y)
REGRESSION ADJUSTED ESTIMATE
CALCULATES FSTIMATES FROM USER DATA USING "EST"
FICTS EASIC OR RETRENCHED GRAPH ON LINE PRINTER
                                                                NAME OF USER WRITTEN ESTIMATING FUNCTION USAGE: FUNCTION NAME (X, N) WHERE X IS A VECTOR WITH N ENTRIES
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E
ELOT (I J) = BLK

CCNT INUE
SET HORIZONTAL XMIN, XMAX
UIH(1) =: 7*NE(1)
UIH(3) =1.2*NE(1)
SET SCALE
CAIL SCALE
(NE(L)
I A ST = -1
I A ST = 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               OF
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DC 80 K=1 I

NEK = NB(K)
FNEK = NE(K)
SECTION & COMPUTE ESTIMATORS FOR SIZE
CALL SECEST(X N M RNEK EST Y KP)
A VERAGE ESTIMATES OF SIZE NE(K) FOR EAU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              EC 10 I=1 M

RH (K I) = 6.

DO 15 J=1.NBK

KP=KP+1

RH (K I) = 1 (KP)

CONTINUE

RH (K I) = FH (K I) +Y (KP)

CONTINUE

RH (K I) = FH (K I) /FLOAT (NBK)

CONTINUE

CALL BCXPRT (Y KP LOCX (K) PLOT RG)

IF (K GT 90 TO 80 TO 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              180
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CALC.
                                                                                                                                                                  DONE
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H
                                                                                                                                                                                                                                                                         ω
                                                                                                                                                                  CAN
                                                                                                                                                                                                                                                                         REFLICATIONS
                                                                                                                                                                  IF D1. LT. 2 THEN NO REGRESSIONS OR PLOTING
                                                                                                                                                                                                                                                                                                                                           )/FLOAI(M)
GO TO 94
I)-M*BA(I)**2)/(M*(M-1.))
                                                                                                                                                                                                                                                                         Σ
                                                                                                                                                                                                                     (EA,RT,BT,L,D1,IX1,IX2)
                                                                                                                                                                                                                                           =ET (KT) *NE (I) ** (KT-1)
                                                                                                                                                                                                                                                                         OVER
                                                                                                                                                                                                                                                                              DO 94 I=1, D1
EA [I] =0.
EV [I] =0.
CC 95 J=1, M
BA [I] =BA [I] +B [I, J] **2
CCNT INUE
EA [I] =BA [I] /F LOA I (M)
IF [M: EQ: { } ] @C TO $ 94
IF [M: EQ: { } ] @C TO $ 94
                                                                                                                                                                                                                                                                         AVERAGE REGRESSION CCEFF.
                                                                                                                                                                               DC 92 K=15 GO TO 113
DC 92 K=15 E
DO 47 S=1, L
                                                                                                                                                                                               DO 47 3=1 L

RT(J) = FH (J, K)

CALL RREG (FA, RT, BT,

B (1 K) = BT {1}

DO 23 KT=2 L

CCNTINUE

CCNTINUE
190
                                                                                                                                                                                                                                                  23
                                                                         8
                                                                                                                                                  80
                                                                                                                                                                                                                                                                                                                                    95
                                                                                                                                                                                                             47
        SOO
                                                                                                                                                           000
                                                                                                                                                                                                                                                                  000
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```
DC 98 I=3 IMIDTH

MAP I FROM DEVICE SPACE TO USER SPACE

UX=(I-DLH(1)) * (ULH(3)-ULH(1)) / (DLH(3)-DLH(1)) + ULH(1)

COMPUTE THE Y VAIUE FROM X AND THE REGRESSION COEFFICIENTS.

UY=BA(1)

CO 99 J=1, L

UY=UY+BA(J+1) / UX**J

CONTINUE
                                                                                                                                                                                                MAP THE Y VALUE FROM USER SPACE TO DEVICE SPACE

J=(UY-ULH(2))*(DIH(4)-DLH(2))/(ULH(4)-ULH(2)) + DLH(2) +

IF(J .LT 1 .OR J .GT .50) GO TO 98

IF(PLOT(I,J) .EQ. BIK) PLOT(I,J)=DOT
                                                                                                                                                                                                                                                                                                                                                                                                                                          A VARIANCE
                                                                                                                                                                                                                                                                                                                       SCALE ASYMETOTE, EETAO AND PLOT ACROSS PLCT.
J= (BA(1) - UIH(2)) * JDLH(4) - DLH(2)) / (ULH(4) - UIH(2)) + DLH(2)
IF (J LT 1 OR 2) GT 50) GO TO TO
DC 120 I=3 INIDTH
IF (PLOT (I, 3) EQ. EIK) PLOT (I, 3) = DASH
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                          WITH
                                                                                                                                                                                                                                                                                                                                                                                                                                        REGRESSION CN VARIANCES PROM EACH SEGMENT
                                                ASYMPTOTE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   V(I) *NE (L) ** (FLOAT (I) /2.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DC 11 1 I=1, I

I F (K.GE.2) GO TO 112

LT=LT-1

K=M*(N/NE(LT))

1 CCNT INUE

2 IF (LT.IT.DI) DT=LT

IF (DT.IT.2) GO TO 113

DC 48 J=1, I

VT (J) = STAT (J,6) * (NE(J) ** 0.5)

8 CCNT INUE

CALL REG (EV, VT, V, LT, DT, IX1, IX2)

DC 77 I = 1, V, I
                                                ESTABLISH REGRESSION LINE &
94 CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      K = M* (N/NE(I))

LT = L

DT = D1

DC 111 I = 1, I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CCNTINDE
                                                                                                                                                                                                                                                                                                                                                                                                         120
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      111
                                                                                                                                                                                                                                                                                            9
8
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TC COMPUT
                                                                                                                                                (STAT (K, 2), K=1, L1)
(STAT (K, 3), K=1, L1)
                                                                                                                                       CCNTINUE

GC TO 14

WRITE (6,157) LABEL (3); (

IT = L1

DC 22 I=1 (IT

DC 22 I=1 (IT

L1 = M (N/NE(L1)), (L1)

IF (K1. GE. 3) GC TO 12
 113
                                 S
                                                                                                            CO
```



```
.4)
SION ON VARIANCE - COEFFICIENTS: ',7X,4G20.6)
SIZE (N): ',15,20X' NO. OF REPLICATIONS (M): ', REGRESSION (D): ',13)
                                                                                                                                                 FICIENTS:

8 X 4620.

9 X, 4620.6
                                                                                                                                                                                                                                                                  FIOT (122,50), DASH, CBAR, CROSS, CSTR, CC, NUM (10) IFLAG
                                                                                                                                                                                                                                                                              /, CBAR/"|"/, CSTR/"*"/, CROSS/"+"/, CO/"0"/
                                                                                                                                                 - COEFFICIENTS: COEFFICIENTS:
                                                                                                                                                                                                                                                 2-D ARRAY
SUBROUTINE EOXPRT (Y, NY, IX, PLOT RG)
FREAL Y (NY), ULH (4), DLH (4)
INTEGER RG
INTEGER*2 FIOT (122,50), DASH, CBAR, CROS
LCGICAL*1 IFLAG
EATA DASH/'-'/, CBAR/'I'/, CSTR/'*'/, CI
                                                                                                   †† ††
                                                                                                                                                                                                          9
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```
NUMBER
                                                                                                                                                                 . LT. XLOW) PLOT (IX, J) = CO
                                                                                                                                      THE
   THE POINTS
                                                                                                                                      AND
                                                                                                                                                    OUTSIDE WINDOW GO TO 30
              FALLS OUTSIDE WINDOW .LT.1) GO TO 8
                                                                                                                                      COUNTED
TO 5
FOINTS JUST SHOW
                                                                                                                                      E
E
                                                                                                                                      T0
                                                                                                                                      RE
                                                                                      YMIN) * VSCALE+1
                                                                                                                                      S
                                                                                                                                      ER S
                                                                                                                         = DASH
= DASH
= DASH
0 UTLINGO TC
                                                                                                              m m
                                                                                                           = CBA |
= CBA |
88
                        8
                                                       S
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                                                                                                                                       O
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```
IINE ENDS UF WITH HI-CRCSS POINTER (LAST FOINT LE [] LE.XHI) IHX=J [] GI:XHI AND:Y[I] LE.CHI) PLOT(IX,J)=CO [] GI:CHI) FLCT(IX,J)=CSTR
                                                                                                                                                                                                                                                                                                                                                                                                                                           LINE ENDS UF WITH HI-CROSS POINTER (LAST FOINT [] LE.XHI) IHX=J [] GI.XHI . AND.Y(I).LE.CHI) PLOT(IX, J) = CO
                                                                                                                                                                                                                                                                                                                                                  (I) GO TO 31
(I) LT.XLOW, PLOT(IX, J) = CC
XLOW, GO TO 26
POINTER (1ST POINT GE XLCW)
                     GE
IF LFLAG .CR. Y (I). IT. XLOW, GO TO 25
THIS IS TEE LOW-CROSS POINTER (1ST POINT
IIX = J
IIX = J
NEXT IINE ENDS UP WITH HI-CRCSS POINTER (
IF Y [I] . LE.XHI) IHX = J
IF Y (I] . GI.XHI . AND. Y (I). LE.CHI) PLOT (IX,
IF Y (I] . GI.XHI . ELCT (IX, J) = CSTR
                                                                                                                                                                                                       INTERQUARTILE + (-) INTERQUARTILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  NUMBER OF OUTLIERS UNLESS K=1,2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PRINT NUMBER OF OUTLIERS UNLESS

DC 22 K=1, 2

IK=II

J= (CLOW-YMIN) *VSCALE + 1

IF (J-LT-0) J=1

IF (K · EQ · 2) IK=III

IF (K · EQ · 2) J= (CHI-YMIN) *VSCALE +

IF (K · EQ · 2) J= (CHI-YMIN) *VSCALE +

IF (J · G T · 5 0) J=5 0

IF (IK · EQ · C) GO TO 22

CALL NUMPRT (IX , J, IK , FLOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FILL BARS AEOVE AND EELOW THE DC 32 I=ILX,IQ1 FLOT (IX, I)=CBAR CCNTINUE CCNTINUE
                                                                                                                                                                                                        10
                                                                                                                                                                                                        SCALE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              96
                                                                                           25
                                                                                                                                                  30
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                26
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REAL*4 YS (E) XS (8 4) BS (4)
REAL*8 Y (8) X (8 4) B (4) XTX (4 4) XTY (4)
** CONVERT FEAL*4 TO REAL*8 ********************

DO 10 I=1 IX1

Y (I) =D B I E (YS (I))

DO 5 J=1, IX2
                                                                                                                                                                                                                                             SUEROUTINE FREG(XSYSBS, M, N, IX1, IX2)
ROBUST REGFESSION CNTAINED IN AN ARRAY OF DIM (IX1, IX2)
Y=M-VECTOR CONTAINED IN AN ARRAY OF DIM (IX1, IX2)
XX, XXI=WORK ARRAYS OF DIM (IX2, IX2)
WY=WORK ARRAY OF DIM (IX2, IX2)
WY=WORK ARRAY OF DIM (IX1, IX2)
XX=WORK ARRAY OF DIM (IX1, IX2)
XY=WORK ARRAY OF DIM (IX1, IX2)
XY=WORK ARRAY OF DIM (IX1, IX2)
XY=WORK ARRAY OF DIM (IX2, IX2)
                                                                                                                                                                                                                                                                                        ENTRY SCALE (ULH DIH)

CCMPUTES X Y SCALE AND LIMITS

X MAX = ULH { 1 }

Y MAX = ULH { 2 }

Y MAX = ULH { 4 }

H SCALE = (DLE (3) -DLH (1) / (ULH (3) -ULH (1) )

N SCALE = (DLE (4) -DLH (2) / (ULH (4) -ULH (2) )

RETURN
           FICT (IX, ILX) = CROSS
FICT (IX, ILX) = CROSS
FICT (IX, IQ1) = DASH
SUM= 0 I = 1 NY
SUM = SUM + Y (I)
SUM = SUM + Y (I)
SUM = SUM - Y (I)
FICT (IX, MEAN) = CSTR
FICT (IX, MEAN) = CSTR
33
                                                                                                                                                                                                            66
                                                                                                                                             0 7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0000000000
```



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***
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NUMPRI PLOIS THE NUMBER IK IN THE 2-D ARRAY PLOT CENTERED THE PLOT (IX, J) POSITION.

IX = COLUMN OF MATRIX PLOT WHERE NUMBER IS TO BE PRINTED.

J = ROW OF MATRIX WHERE MUMBER IS TO BE PRINTED.

IK = NUMBER TO BE PRINTED

FLOT = 2-D ARRAY WHERE NUMBER IS TO BE PLOTED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INTEGER*2 NUM 10) FLCT 1122 50)

IF (IK.LT.10) GO TO 1

IF (IK.LT.100) GO TO 2

IF (IK.LT.100) GO TO 3

IF (IK.LT.1000) GO TO 3

IF (IK.LT.1000) GO TO 3

IF (IK.LT.1000) GO TO 4

I 100 0 = IK.10000 $10000 $10000 $1000

FLCT (IX.2 3) = NUM (I 10000 $1000 $1000

FLCT (IX.10000 $10000 $10000 $10000 $1000

FLCT (IX.10000 $10000 $10000 $10000 $1000

FLCT (IX.10000 $10000 $10000 $10000 $1000 $1000

FLCT (IX.1000 $10000 $10000 $10000 $1000 $1000 $1000

FLCT (IX.1000 $10000 $10000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1000 $1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SUBROUTINE NUMPRT (IX, J, IK, PLOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                       C***** CONVERT FEAL*8 TO REAL*4
DO 15 J=1 I X2
BS (J) = SNGL (E(J))
CONTINUE
CONTINUE (XS (I, J))
                                                                                                                                                                                                                                                                                       MATSO (X
MATHOI (S
CHOLES (X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               FETURN
END
```

00000000



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Z
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SUEROUTINE MAXMIN (Y, N, YMAX, YMIN)
RETURNS MAX AND MIN'VALUES'OF VECTOR Y OF LENGTH
REAL Y (N)
YMAX = Y (1)
YMIN = Y (1)
YMIN = Y (1)
DC 605 J=1 N
IF(Y(J) - L1 · YMIN) YMIN = Y (J)
                                                                                                                                                                                                                                                                                                                SUBROUTINE SECEST (X N, M, NEK, EST, Y, KF)
FEAL X (5000C) Y (12500)
COMPUTE ESTIMATES "EST" FOR SECTION LENGTH NEI
NEK=N/NEK
KF=0
DC 10 I=1 (#
FICT (IX, J) = NUM (I10+1)

I1 = (IK-I1000*1000-I100*100) /10

ELCT (IX+1, J) = NUM (I1+1)

GC TO 22

I100 = TK/10
                                                                                   3 I 100 = IK/100

E I OT (IX-1, 3) = NUM(I100+1)

I 10 = (IK-1100*100)/10

E I CT (IX-1) = NUM(I10+1)

I 1 = (IK-1100*100)/10

E I CT (IX+1, 3) = NUM(I10+1)

G C T O 22

I 10 = IK/10

E I CT (IX-10) = NUM(I10+1)

I 1 = (IX-10) = NUM(I11+1)

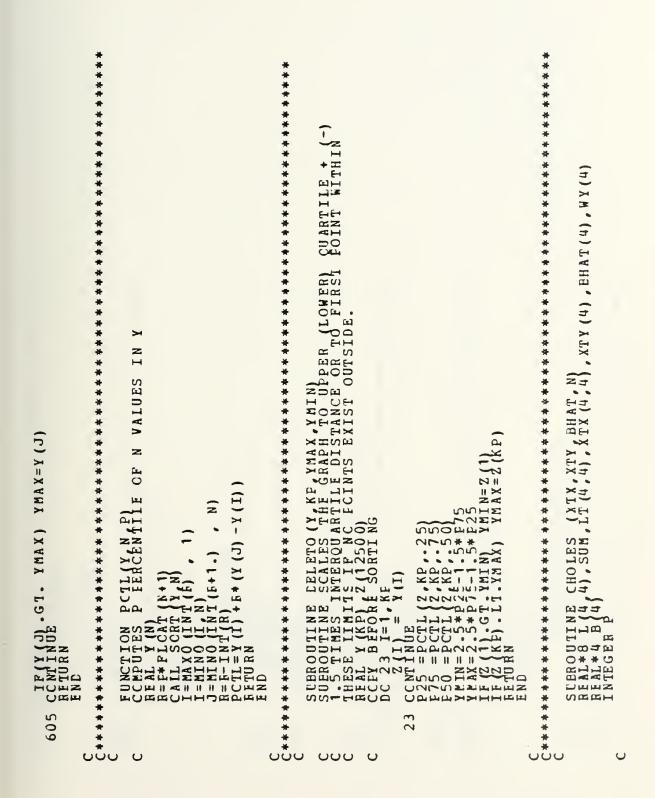
G C T O 22

I 1 = (IX-10) = NUM(I11+1)

G C T O 22

I I = (IX-10) = NUM(I1+1)
                                                                                                                                                                                                                                                                                                                                      22
                                                                                     (*)
                                                                                                                                                                           ()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     C
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***************** LI NI
   *****
                                                                                                                                                                                                                                                                                                             ***
                                                                                                                                                                                                                                 ***
                                                                                         4
                                                                                                                                                                                                                                            WY (1) = XTY (1) /L (1, 1)

DO 700 I= 1-1

SUM=0.0 CC

DO 600 C= 1, II

SUM=SUM+(WY (J)*L (I, J))

CONTINUE

WY (1) = (XTY (I) - SUM) /L (I, I)

CONTINUE
EHAT (1) = 0.CD0
DO 50 J = 1.N
L(1 J) = 0.CD0
LT (1 J) = 0.0D0
LT (1 J) = 0.0D0
CCNT INUE
ALGORITHH DECOMPOSITION
KEEK - 1
DO 500 J = 1.KK
                                                                                                                                                                                                                                 PART
                                                                                                                                                                                                                                                                                                             X
                                                                                                                                                                                                                                                                                                              H
                                                                                                                                                                                                                                                                                                             PHA T
                                                                                                                                                                                                                                                                                                700
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XRES
                                                                                                                                                                                       11
                                                                                                                  SUPROUTINE MATSO (X, XRES, M, N) REAL * 8 X (8,4), XT (4,8), XRES (4,4), SUM
CBROUTINE EATMUL ( X,Y,XTY,H,N)
EAL*8 Y(8),XT(4,8),X(8,4),XTY(4)
                                                                                                      MATRIX MULTIPLICATION
                                                                                                                                     X-TEANSPOSE IN LT
                                                                                                                                                                                                                                                                    MATRIX MULTIPLICATION
                                                           DC 950 I=14
B(I)=SNGI (BHAT (I))
CCNTINUE
                                                                                                                                                                                                                      CCNTINUE
FETURN
                                                                                                                                    EUILD X-TE
DO 20 I=1 L
DO 10 15 =1
CONTINUÉ
CCNTINUE
                                                                                     RETURNEND
                                                                                                                                                                                            DC
                                                                                                 *
*
*
*
                                                                                                                                                                                                                                                                    ****
                                            600
                                    750
                                                                        0 2 5
```



```
****
                                     ******
                                                                                                                        ****
                                                                                                                                                                                         .GT.Y(KK))) GO TO 100
                                                                                                                 SUEROUTINE SORT (YN)
INPLACE SORT USING SHELL ALGORITHM
FEAL Y(N) TEMP
INTEGERGAE
ICGICAL EXCH
                        500
                                                                                                                                                GAP= (N/2)

IF (.NCT. (GAP.NE.O)) GO TO 53

EXCH=.TRUE.

K=N-GAP

DO 2 CC I=1, K

KK=I+GAP

IF (.NCT. (Y I).GT.Y (KK)

Y (I)=Y/X (KK)
                                                                                                                                                                                                    CONTINUE
CONTINUE
CONTINUE
GAP=(GAE/2)
GC TO 5
CCNTINUE
      CCNTINUE XT
                                                                                                                                                                                                                                                           FETURNEND ND
                               *
*
*
*
*
UU
*****
                                                                                                                                                                                                                                                500
C
                                                                                                                                                                                                                     100
                                                                      40
                                                                                 50
                                                                                                                                                        20
                                                                                                                                              C
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SIMTE2 PROGRAM LISTING

TO GENERATE REGRESSION ADJUSTED ESTIMATES AND BCX PLCTS OF ESTIMATES OF AN INPUT RAW DATA SERIES X CONTAING (REFLICATIONS) OF N VALUES EACH. UP TO 3 ESTIMATING FUNCTIONS CAN BE USED. THE GRAPHS CAN ALL PE OF THE SAME SCALE OR SCALED INDIVIDUALLY.	ICN OF PARAMETERS	REPI*4 ARRAY CONTAINING DATA. A MAXIMUM OF 50,000 DATA ELEMENTS CAN BE STORED IN X.	NUMBER OF DATA ELEMENTS PER SECTION (N IS SAMPLE SIZE). N CANNOT EXCEED 50,000 AND M*N MUST NOT EXCEED 50,000.	NUMBER OF SECTIONS (REPLICATIONS). M CANNOT EXCEED 100 AND M*N MUST NOT EXCEED 50,000.	INTEGER ARRAY OF SIZE 8 CONTAINING SUBSAMPLE SIZES FCR N. THE VALUES OF NE MUST BE FROM SMALLEST TO LARGEST. NO FLEMENT OF THE ARRAY NE CAN BE GREATER THAN N. M*(N/NE(1)) MUST NOT EXCEED 12,500.	NUMEER OF SUBSAMPLE SIZES FROM NE(8) THAT WILL BE USED TO SECTION N. IT IS ALSC THE NUMBER OF BOXPLOTS THAT WILL BE FRODUCED.	DEGREE OF REGRESSION FOR MEAN AND VARIANCE REGRESSIONS. D WILL BE REDUCED BY RAGE IF THE SAMPLE IS NOT LARGE ENCUGH. D MUST BE 1,2 OR 3. D=0 WILL IGNORE REGRESSIONS.	*** SCALING *** SCALING IS ACCOMPLISHED BY TAKING THE SMAILEST AND THE IARGEST ESTIMATE VALUES FROM ALL ESTIMATING FUNCTIONS IARGEST ESTIMATE VALUES FROM ALL ESTIMATING FUNCTIONS ND FROM FOF ALL SUBSAMPLE SIZES. THE SEI PARAMETER ALLOWS THE USER TO SCALE THE GRAPH CF EACH ESTIMATOR INDIVIDUALLY OF TC SCALE THEM ALL TO THE SAME SCALE IS ACCOMPLISHED BY TAKING THE MINIMUM AND MAXIMUM ESTIMAT FROM ALL THE ESTIMATORS USING NE (1) SUBSAMPLE SIZE. THE RG FARAMETER ALLOWS THE USER TO RREDUCE THE VERTICAL SCALE TO: THE UPPER QUARTILE LISTANCE + 1.5 TIMES INTERQUARTILE DISTANCE AS THE MAX VALUE AND THE LOWER
FUFFCSE	DESCFIPTI	×	z	æ	ш Z	П	Ð	



CUARTILE - 1.5 TIMES THE INTERQUARTILE DISTANCE AS THE MIN VALUE. THE INTERQUARTILE DISTANCE IS COMFUTED FROM THE SAMPLE OF ESTIMATES FROM THE NE (1) SUBSAMFLE SIZE. IF THERE ARE NO ESTIMATES OUTSIDE THESE MIN AND MAX VALUES THEN THE SCALE IS TO THE FIRST VALUE WITHIN. IF THERE ARE ESTIMATES OUTSIDE THESE LIMITS THEN THEY ARE COUNTED AND THE NUMBER PRINTED AT THE ENDS OF THE ECX PLOTS. SCALE. WHEN THE VERTICAL SCALE IS SET THE SEI PARAMETER IS IGNORED AND THE VERTICAL SCALE BECCHES YMIN AND YMAX	RG=0 DO NOT REDUCE THE VERTICAL SCALE OF THE GRAPHS. RG=1 REDUCE GRAPHICS VERTICAL SCALE TC UPPER (LOWER) QUARTILE + (-) INTERQUARTILE DISTANCE.	SEI=0 DO NOT SCALE ESTIMATORS' GRAFHS INDIVIDUALLY. SEI=1 SCALE ESTIMATORS' GRAPHS INCIVICUALLY.	SVS=0 PROGRAM WILL CALCULATE VERTICAL SCALE. SVS=1 USER SETS VERTICAL SCALE TO YMIN AND YMAX.	LOW VALUE OF VERTICAL SCALE. SET BY USER WHEN SVS=1	HIGH VALUE OF VERTICAL SCALE. SET BY USER WHEN SVS=1	NUMEER OF ESTIMATORS THAT WILL BE USED TO CALCULATE STATISTICAL FARAMETER FROM X DATA. NEST MUST BE 1,2 OR 3.	NAMES OF THE ESTIMATOR FUNCTIONS THAT WILL EE USED TO CALCULATE THE STATISTICAL PARAMETER. CALL SEQUENCE ON EACH FUNCTION IS: CALL FNAME (X,N) WHERE X IS THE DATA ARRAY AND N IS THE NUMBER OF DATA PCINTS. THEY MUST BE DECLARED IN THE CALLING ERGGRAM (RAGE) IN THE ORDER THEY ARE USED. DUMMY VARIABLES MUST BE INSERTED WHEN THERE ARE LESS THAN 3 ESTIMATORS.	TITLES ASSOCIATED WITH EACH ESTIMATOR (EST1,2,3). A MAX OF 120 CHARACTERS CAN BE USED TO DESCRIEE EACH ESTIMATOR. EACE TITLE MUST BE DECLARED AS REAL*8 (15) ARRAYS UNLESS PASSED AS AN ARGUMENT OF THE CALLING FROGRAM RAGE. WHEN PASSING THE TITLE AS AN ARGUMENT THERE MUST BE A MINIMUM OF 120 CHARACTERS BETWEEN APCSTROPHES.	经备款条件 化苯基苯酚 计 医生物 医生物 医生物 医乳球
	RG	SEI	SVS	Y MIN	Y H AX	NEST	EST2 EST3	TTL1 TTL2 TTL3	* * * * *



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TELL D, RG, SEL, SVS, YHIN, Y MAX, NEST, EST1, (12560)
                                                                                                                                                                                                                                                                                                                                                                                                                 SH=NE (1)

IF (LT. EQ. 0) GO TO 13

IF (LT. EQ. 0) GO TO 13

IF (LT. EQ. 0) GO TO 13

IF (NE (I) GT.NE (I1)) WRITE (6,110)

IF (NE ST. EQ. 1.0R.N EST. EQ. 2.0R.NEST. EQ. 3) GO TO GO TO EQ. 1 E ST. EQ. 1.0R.N EST. EQ. 1.0R.N EST. EQ. 3) GO TO EQ. 1 E ST. EQ. 1.0R.N E. 100) GO TO EQ. 1 E ST. EQ. 1.0R.N E. 100) GO TO EQ. 1 E ST. EQ. 1.0R.N E. 100) GO TO EQ. 1 E ST. EQ. 1.0R.N E. 100) GO TO EQ. 1 E ST. EQ. 1.0R.N E. 10R.N E. 1
                                                                                                                                    SUBROUTINE SIMTB(X N N P TILL, EST2, TIL2, EST3, TI R EAL X (IR IFK), ULH(4), R FAL*8 TTL1(15), TTL2(1), INTEGER NE(8), R6, SEI SINTEGER D, I, NEST, TEST
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PAIR***
                                                                                                    PAIR**
                                                                                                                                                                                                                                                                                    VECTOR
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                                                                                                                      IRK)
                                                                                                                                                                                              RK)
                                             RK)
                                         · .ZZ
                                                                                                                       MZZ
                                                                                                                                                                                               KZZ
      UIH (2) =1.E30
UIH (4) =-1.E30
LEFIND VERTICAL SCALE FOR 1ST ESTIMATOR.
CALL SECEST (X N M NE (IK) EST 1 Y KP IR
IF (RG.E0.1) CALL BELETO (Y KP YMAX, YMIN
IF (YMIN .II. ULH (2) ) ULH (2) = YMIN
IF (YMAX .GI. ULH (4) ) ULH (4) = YMAX
                                                                                                 FIND VERTICAL SCALE FOR 2ND ESTIMATOR, CALL SECEST(X N M NE (IK) EST2 Y KE IE IF (RG.EQ.1) CALL DELETO (Y KP, YMAK, YMIN IF (YMIN . IT. ULH (2)) ULH (2) = YMAX, YMIN IF (YMAX . GT. ULH (4)) ULH (4) = YMAX
                                                                                                                                                                           ESTIMA TOR
                                                                                                                                                                                              HHH
                                                                                                                                                                          FIND VERTICAL SCALE FOR 3RD ESTIMATOR CALL SECEST(X N M NE(IK) EST3 Y KP, I F (RG.EQ.1) CALL DELETO(Y, KP, YMAK, YM) IF (RG.NE.1) CALL MAXMIN (Y, KP, YMAK, YM) IF (YMAX .GT. ULH (2)  ULH (2) = YMAX OCHINUE RETURN CALCULATED SCALE TO CALLER YMAX = ULH (4)
                                                                                                                                                                                              K P,
YA
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FCEMAT (1X "ESTIMATOR: "15A8)
FCEMAT (1X "VERTICAL SCALE: YMIN = "F10.4"/18X "YMAX = "F10.4"/FCEMAT (*** ERROR. L MUST BE AN INTEGER EETWEEN 1 AND 100.
FCEMAT (*** ERROR. M*N EXCEEDS 50.000 ****)
FCEMAT (**** ERROR. NEST MUST BE 3 OR LESS. ***)
FORMAT (**** ERROR. NEST MUST BE 3 OR LESS. ***)
FORMAT (**** ERROR. NEST MUST BE 1 OR GREATER TO COMPUTE STATISTICS. "/"
FCEMAT (**** ERROR. D MUST BE LESS THAN OR ECUAL TC 3 ****)
FCEMAT (**** WARN ING. NE ARRAY ELLEMENTS ARE NOT IN ORDER (****)
FCEMAT (**** WARN ING. NE ARRAY ELLEMENTS ARE NOT IN ORDER (****)
FCEMAT (**** WARN ING. NE ARRAY ELLEMENTS ELEMENT SCALE.)
          GRAFH
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RK)
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          0-
FIND VERTICAL SCALE FOR 1ST ESTIMATOR AND IF (RG - EQ - 1) CALL BELETO (Y, KP, YMAX, YMIN) IF (RG - NE - 1) CALL BELETO (Y, KP, YMAX, YMIN) UIH(2) = YMIN UIH(4) = YMAX (YMIN) UIH(2) (VIH(4) UIH(4) = YMAX (YMIN) UIH(2) (VIH(4) UIH(4) = YMAX (YMIN) UIH(4) = YMAX (YMIN) UIH(4) = YMAX (YMIN) UIH(4) 
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FIND VERTICAL SCALE FOR 2ND ESTIMATOR AND USE (SECEST (XN M NE (1) EST2 Y KP, IR IN IF (RG. NE.1) CALL BELETO (Y, KP, YMAX, YMIN) UIH (4) = YMIN UIH (4) = YMAX (MIN) UIH (4) UIH (5) UIH (4) UIH (4) UIH (5) UIH (4) UIH (5) UIH (4) UIH (5) U
   E FOR 1ST ESTIMATOR A NE (1) EST1 Y KP IRIR ELETO (Y KP, YMAX, YMIN) AX MIN (Y KP, KP, YMAX, YMIN)
                                                                                                                                                                                                                                                                              Œ
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Numest2, Ne. L, RG, D, ULH, Y, III
TTL2
3) GO TO 80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  G, D, ULH, Y, I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FIND VERTICAL SCALE FOR 3RD ESTIMATOR

IF (SVS.EQ.1) GO TO 78

CALL SECEST (X N M NE (1) EST3 Y KP IR

IF (RG.EQ.1) CALL MAXMIN (Y, KP, YMAX, YMIN

UIH (4) = YMIN

UIH (4) = YMAX

CALL PRST (X, N, M, EST3 NE, L, RG, D, ULH, Y, IM

WRITE (6, 102) TTL3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        HHH
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ORDE
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NTEGER NB (E) LOCX (8) D1 IWIDTH, UD, D, LT, ET, RG, RNEK

NTEGER*2 FIOT (122,50), CBAR, BLK, DASH, CSTR, NUM (10), DOT

NTEGER*2 FIOT (122,50), CBAR, BLK, DASH, CSTR, NUM (10), DOT

NTEGER*2 FIOT (122,50), CBAR, BLK, DLH (4), Y (12500)

NTEGER*3 FIOT (100), STAT (8,6), VT (8)

NTEAL*4 RH (8,10), STAT (8,6), VT (8), NT (8), ET

NTEGER*3 FIOT (100), STAT (8,6), NT (8), NT (8), ET
                                                                                                                                                                                        BE <= 10000)
AIUES EACH
                                                                                                                                                                                                                                                                               124
              ***
                                                                                                                                                                     NO. OF FEPLICATIONS (MUST BE <= 100)
NUMBER CF VALUES IN EACH REPLICATION (M*N MUST BE <= 100
USERS VECTOR WITH M CONSECUTIVE BATCHES OF N VAIUES EACH
NO. OF SECTION SIZES (MUST EE BETWEEN 1 AND 8)
ARRAY WITH THE L SUBSAMPLE SIZES (MUST BE IN ASCENDING
DEGREE OF THE REGRESSION (MUST BE <= 3 & <= 1-1)
XMIN, XMIN, XMAX, YMAX IN USER UNITS
ONLY ULH(2) AND ULH(4) NEED TO BE PASSED. OTHERS CALC.
                                                                                                                                                                                                                                                                                                                                                                                                                      EATA DLH/1.122.50

DATA BLK/. '', 'DASH/'-'/' STD'', 'STD MEAN', 'SKEWNESS', 'KURTOSIS'/
DATA LABEL ''MÉAN', 'STD', 'STD MEAN', 'SKEWNESS', 'KURTOSIS'/
IX1=8
IX2=4
IX2=4
IX2=4
IX1=B+1
IWIDTH=IFIX (DLH(3))
EUILD REGRESSION MATRICES FOR AVERAGES AND VAFIANCES
DC 84 K=11
I DD 86 J=1 LD
T=FLOAT (KF(L)) / FLOAT (NE(K))
RA (K,J) = 1** (FLOAT (J))/2.0)
86 CONTINUE
RA (K,J) = 1** (FLOAT (J))/2.0)
86 CONTINUE
CLEAR FLOT
ARRAY
                                                                       FUNCTIO
              *****************************
                                        FRST(X N, M, EST NE, I, RG, UD, ULH, Y, IR, IFK)
ALJUST ED FSTIMATE
FSTIMATES FROM USER DATA USING "EST" FU
C OR RETRENCHED GRAFH ON LINE PRINTER
                                                                                                                WRITTEN ESTIMATING FUNCTIO
UNCTION NAME (X,N)
VECTOR WITH N ENTRIES
                                                                                                                 KHK
                                                                                                                AGE: USER
              **
              ****
                                        SUBROUTINE
REGRESSION
TALCULATES
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-UIH(1) * (DLH(3) -DLH(1)) / (ULH(3) -ULH(1)) +DLH(1) +.5
LAST+4 LOCX(K) = LAST+4
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FLOT (I S) = ELK

CONTINUE

SET HORIZONTAL XMIN, XMAX

UIH (3) = 1, 2 * NE (1)

SET SCALE

CALL SCALE (ULH, DLH)

CCMP UTE LOCATION CF EOXPLOTS ALONG X-AXIS

I AST = -1

LOS SET SCALE

CALL SCALE

C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IR IRK)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DC 80 K=1, I

NEK=NE(K)

FNEK=NE(K)

SECTION & COMPUTE EST

CALL SECEST(X N M, RNI

AVERAGE ESTIMATES OP

KF=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              180
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CHECK TO INSURE SAMFIE SIZE IS LARGE ENOUGH FCR
EACH MOMENT COMPUTATION.

IF (KP.LT.2) GO TO 7

VAR = SUM2 / (KP - 1.0)

SIDV = SQRI (VAR)

I F (KP.LT.3) GO TO 8

XSUM = SNGI (SUM3) * KP / ((KP-1.) * (KP-2.))

SKEW = XSUM4 - VAR*VAR*3.* (KP-2.) * (KP-1.) * (KP-2.) * (KP-3.))

SKEW = XSUM4 - VAR*VAR*3.* (KP-1.) * (KP-2.) * (KP-2.) * (KP-3.)

SIDV | SIDV | SYUM4 - VAR*VAR*3.* (KP-1.) * (KP+E-3.) / (KP+C.) * (KP-2.) * (KP-2.) * (KP-2.) * (KP-2.) * (KP-3.)

SIAT | K, 3 = SIDV | SORT (FLOAT (KP))

SIAT | K, 4 = SKEW | SKEW | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SIAT | K, 6 = VAR | SKEW | SKEW
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         uv 47 5=1,L

RT(J) = H(J,K)

CALL RREG (FA,RT,BT,L,D1,IX1,IX2)

E(T,K) = BT (T)

D(J 23 KT = 2,L)

B(KT,K) = ET(KT) *NE(L) ** (KT-1)

23 CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF D1. LT. 2 THEN NO REGRESSIONS OR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Σ
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CCNTINUE
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DC 98 I=3 INIDTH

MAP I FROM DEVICE SPACE TO USER SPACE

UX= (I-DLH (1)) * (UIH (3) ~ ULH (1)) / (DLH (3) - DLH (1)) + ULH (1)

COMPUTE THE Y VALUE FROM X AND THE REGRESSICN COEPPICIENTS.

UY= BA (1)

CO 99 J= 1, E

UX= UY+ BA (J+1) / UX**J

CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       A VARIANCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MAP THE Y VALUE FROM USER SPACE TO DEVICE SPACE

J= (UY-ULH(2)) * (DIH(4) - DLH(2)) / (ULH(4) - ULH(2)) + DLH(2)

IF (J .LT 1 .OR. J .GT . 50) GO TO 98

IF (PLOT(I.J) .EQ. BIK) PLOT(I.J) = DOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     WITH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 REGRESSION CN VARIANCES FROM EACH SEGMENT
                                                                                                                                                                                                        ASYMPTOTE
EV_{I} = (BV_{I}) - M*BA(I) **2) / (M*(M-1.))
ES_{I} = BV_{I} **.5
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               V(I) *NE (L) ** (FLOAT (I) /2.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               117 K=M* (N/NE(I))

LT=L
LT=L
LT=L
LT=LT-1

I F (K, GE. 2)
CO TO 112

LT=LT-1

I F (LT-LT-1)

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                                                                                                                                                                                                        ESTABLISH FEGRESSION LINE
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FIOT
113
     90
       115
          130
CO
              S
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FIOT (122,50), DASH, CBAR, CROSS, CSTR, CC, NUM (10)
                                                                                                                                                                SUEROUTINE EOXPRT (Y, NY, IX, PLOT, RG)
PREPARES BCXPLOT FECM VECTOR Y (IN 2-D ARRAY PLOT)
FFAL Y (NY), ULH (4), DIH (4)
INTEGER RG
INTEGER*2 FIOT (122,50), DASH, CBAR, CROSS, CSTR, CC, NUM (
ICGICAL*1 IFLAG
                                                                         77 77
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PRINTEL.
EATA DASH '-'CBAR''', CSTR'**, CROSS/'+', CC/'0'/
IF (NY 'GE' 5) GO TO 5

WHEN LESS TEAN 9 FOINTS JUST SHOW THE POINTS

DC 8 I=1, NY

J= (Y (I) -YMIN) *VSCALE + 1.

IGNORE VAIUE IF IT FALLS OUTSIDE WINDOW

IF (J GT' 5C OR. J.LT'') GO TO 8

CCNTINUE

SUM=SUM+Y (I)

B CCNTINUE

SUM=SUM+Y (I)

MEAN = (SUM-YMIN) *VSCALE+1

FICT (IX MEAN) = CSTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            NUMEER
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= DASH
= DASH
= DASH
OUTLIERS
GO TO 55
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IQ3
= CBAR
= CBAR
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FICT HX+1
FICT HX+1
DE TERMIN-1
TO SO I ED ON OR I E ON 
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LINE ENDS UP WITH HI-CROSS POINTER (IAST FOINT LE []). LE.XHI) IHX=J []. GT.XHI . AND.Y(I). LE.CHI) PLOT(IX, J) = CO NUE
                                                                                                                                                                                                                               UP WITH HI-CROSS POINTER (LAST FOINT IHX=J
IHX=J
• AND Y (I) • LE CHI) PLOT (IX, J) = CO
FLOT (IX, J) = CSTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          TO INTERQUARTILE + (-) INTERQUARTILE DISTANCE
AND. Y (I) LT. XLOW) PLOT (IX, J) = CO (I) LT. XLOW) GO TO 25 CRCSS POINTER (1ST POINT GE XLCW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (I) GO TO 31
(I) LT.XLOW) PLOT(IX,J)=CO
(LOW) GO TO 26
OINTER (1ST POINT GE XLCW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        0
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             NUMBER OF OUTLIERS UNLESS K=1,2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FRINT NUMBER OF OUTLIERS UNLESS

IK=II
J= (CLOW-YMIN) * VSCALE + 1

IF (J.LT.0) J=1

IF (K.EQ.2) IK=III

IF (K.EQ.2) J= (CHI-YMIN) * VSCALE +

IF (IK.EQ.2) J= (CHI-YMIN) * VSCAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      THE
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CC 32 I=ILX,IQ1

FLOT (IX,I)=CBAR

CCNTINUE

DC 33 I=IQ3,IHX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SCALE
                                                                                                                                                                                                                                                                                                                                                                                                                                           30
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EIOT (IX, I) = CBAR

CCNTINUE
FICT (IX, ILX) = CROSS
EIOT (IX, ILX) = CROSS
EIOT (IX, IQ1) = DASH
ELOT (IX, IQ2) = CROSS
EIOT (IX, IQ3) = DASH
EOUT (IX, IQ3) = DASH
SUM = SUM + Y (I)
CCNTINUE
SUM = SUM / Y (I)
CCNTINUE
SUM = YMIN) *V SCALE+1
FLOT (IX, MEAN) = CSTR
CCNT (IX, MEAN) = CSTR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 REAL*4 YS (8) X (8 4) BS (4)
REAL*8 Y (8) X (8 4) BS (4)
** CONVERT FEAL*4 TO REAL*8 ***************
DC 10 I=1 IX1
Y (I)=DBIE (YS(I))
DO 5 J=1 IX2
X (I,J)=DBIE (XS(I,J))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SUBROUTINE FREG(XS, YS, BS, M, N, IX1, IX2)

KCEUST REGRESSION ON Y=X*B

X=M BY N MATRIX CONTAINED IN AN ARRAY OF DIM(IX1, IX2)

Y=M-VECTOR CONTAINED IN AN ARRAY OF DIM(IX1)

XX, XXI=WORK A FRAYS OF DIM(IX2, IX2)

WY=WCFK ARRAY CF DIM(IX1)

WX=WCFK MATRIX OF DIM(IX1)

XY=WORK ARRAY CF DIM(IX2)

XY=WORK ARRAY CF DIM(IX2)

WK=WCRK ARRAY CF DIM(IX2)

XY=WORK ARRAY CF DIM(IX2)

WK=WCFK ARRAY CF DIM(IX2)
                                                                                                                                                                                                                                                                                                                     ENTRY SCALF (ULH, DIH)

CCMPUTES

X MIN=ULH (1)

X MAX = ULH (2)

Y MAX = ULH (4)

FETURN

ETURN
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NUMPRT PLOTS THE NUMBER IK IN THE 2-D ARRAY PIOT CENTERED THE PLOT (IX, J) POSITION.

IX = CCLUMN OF MATRIX PLOT WHERE NUMBER IS TO BE PRINTED.

J = ROW OF MATRIX WHERE MUMBER IS TO BE PRINTED.

IK = NUMBER TO BE PRINTED

FLOT = 2-D ARRAY WHERE NUMBER IS TO BE PLOTED.
                                                 NUM (10) PLCT (122 450) 5., '6', '7', '8', '9'/ 10' GO TO 2 1000) GC TO 3 10000) GC TO 4 4 K/10000
                                                                                                                            SUEROUTINE NUMPRT (IX, J, IK, PLOT)
                       MATSO
MATMUI
CHOLES
CCNTINUE
                                                                                       RETURN
END
                       CALL
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MATCH 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                             VALUE OF IRK2.)
                                                                                                                                                                                                                                                                                                                                                                                                                   LON
                                                                                                                                                                                                                                                                                                                                                               FRK2) GO TO 20
6,2)
(13, *** ERROR IN SUBROUTINE SECEST ***)
                                                                                                                                                                                                                                                                                                                                                                                                                  X, "SECOND DIMENSION OF ARRAY XW DCES
                                                                                                                                                                                                                                                                                                       CCMPUTE ESTIMATES "EST" FOR SECTION LENGTH NEK *** IRK2 MCST MATCH THE SECOND DIMENSION OF XW LATA IRK2/ 3/ DATA IDR /5000/
                                                                                                                                                                                                                                                                    SUBROUTINE SECEST (X N M, NEK EST, Y, KP, IR, IRK) REAL X (IR, 1FK), Y (12506), XW (5000, 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                             O
Z
(4) = NUM (110+1)

(K-11000*1000-1100*100-110*10)

(+1,3) = NUM (11+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                         A
                                                                                                                                                                                                                                                                                                                                                                                                                                           "CHANGE DIMENSION
                                                                                                                                             = NUR(I10+1)
*10)
                                                                                                                                                                     = NUM (I1+1)
                                                                                                                                                                                             = NUM (IK+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      NBK=N/NEK

KF=0

DC 100 I=1, M

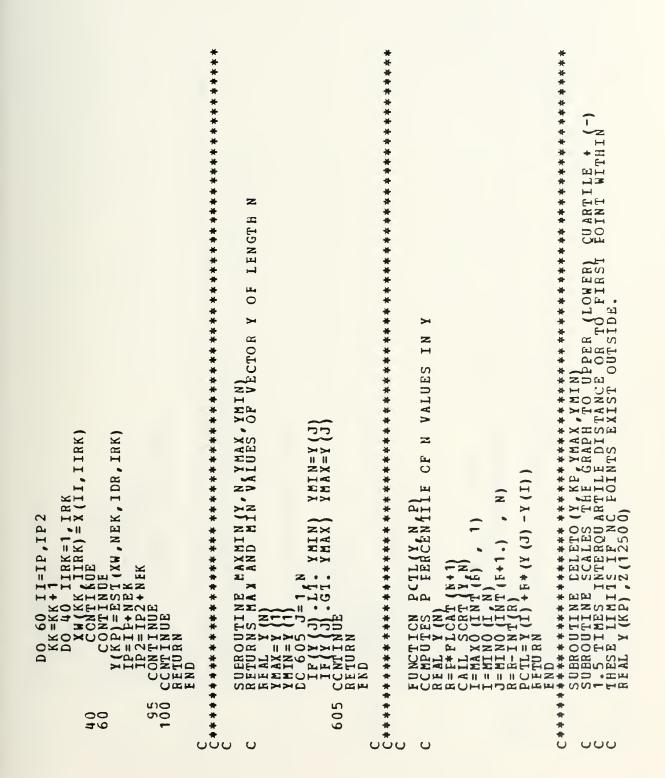
IF= (I-1) *N + 1

IP2=IP+NEK

CO 95 J=1, NBK

KF=KF+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                       SICP
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CCEY BEFORE SORTING

DO 23 I=1 KF

Z (I) = Y(I)

Z (I) = Y(I)

Z (I) = Y(I)

Z (I) = Y(I)

Y (I) = Y(I)

Y (I) = Y(I)

Y (I) = PCTL (Z (KP) - 75)

F 5 = PCTL (Z (KP) - 75)

F 5 = PCTL (Z (KP) - 75)

Y (I) = PCTL (Z (KP) - 75)

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              C **** INIT L **********

DC 100 I=1, N

EHAT (1) = 0. CD0

EC 50 J = 1. N

I (1 J) = 0. CD0

IT (1 J) = 0. CD0

CCNTINUE

CCNTINUE

CCNTINUE

CONTINUE

SUM = 0. 0 D 0

SUM = 0. 0 D 0

IF (1 J) = 0.
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                                                                                                                                                                                     XRES
                                                                                                                                                                                                             X-TFANSPOSE IN LT *******
                                                                                                                                                                                              SUEROUTINE MATSQ (X, XRES, M, N) REAL * 8 X (8,4), XT (4,8), X RES (4,4), SUM
                                                                                            PART
                                                                                                                                                                                    MATRIX MULTIPLICATION
                                                                                                                                                DC 950 I=1 4
B(I)=SNGI (BHAT (I))
CCNTINUE
 Z
                                                                                                                                                                      RETURNENE
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                                                                                                                                                           950
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**
                                                                                                                                   XIX
                                                                                                                                                 SUEROUTINE MATMUL (X,Y,XTY,M,N)
REAL*8 Y(8),XT(4,8),X(8,4),XTY(4),SUM
30 CCNTINUE ESC (1, J) = SUM END
                                                                                                                                    II
                                                                                                                                                                                                                                                                                                                                                SUEROUTINE SORT (Y,N)
INFLACE SORT USING SHELL ALGORITHM
REAL Y(N), TEMP
INTEGER GAF
ICGICAL EXCE
                                                                                                                                  **** MATRIX MULTIPLICATION XT * Y
                                                                                                                                                                                                                                                DC 50 I=1 N

SUM =0.0 E0

DO 40 J=1, M

SUM = SUM + (XT (I, J) *Y(J))

CONTINUE

XTY (I) = SUM

FETURN

END
                                                                                                                                                                        +* BUILD XT *****

DO 20 I=1 E

DO 10 10 J=1 N

XT (J I) = X (I, J)

CONTINUE
                                                                                                                                                                                                                                 XT * Y = XTY
                                                                                                                                                                                                                                                                                                                                                                                                GAF= (N/2)
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LISTING FROGRAM SIMTE3



CF EACH ESTIMATOR INDIVIDUALLY CR TC SCALE THEM ALL TO THE SAME SCALE IS ACCOMPLISHED BY TAKING THE MINIMUM AND MAXIMUM ESTIMATE FROM ALL THE ESTIMATORS USING NE(1) SUBSAMPLE SIZE. THE RG FARAMETER ALLOWS THE USER TO RREDUCE THE VERTICAL SCALE TO: THE UPPER QUARTILE DISTANCE + 1.5 TIMES INTERQUARTILE DISTANCE + 1.5 TIMES INTERQUARTILE DISTANCE STIMATES THE INTERQUARTILE DISTANCE AS THE MAX VALUE AND THE LOWER SIZE. THE SAMPLE OF ESTIMATES FROM THE NE(1) SUBSAMFLE SIZE. IF THERE ARE NO ESTIMATES OUTSIDE THESE MIN AND MAX VALUES THEN THE SCALE IS TO THE FIRST VALUE WITHIN. IF THERE ARE ESTIMATES OUTSIDE THESE WITHIN. ECX PLOIS.	THE SV CALE. WH S IGNORE	RG=0 DO NCT REDUCE THE VERTICAL SCALE OF THE GRAPHS. RG=1 REDUCE GRAPHICS VERTICAL SCALE TC UPPER (LOWER) QUARTILE + (-) INTERQUARTILE DISTANCE.	SEI=0 DO NOT SCALE ESTIMATORS GRAFHS INDIVIDUALLY.	SVS=0 PROGRAM WILL CALCULATE VERTICAL SCALE. SVS=1 USER SETS VERTICAL SCALE TO YMIN AND YMAX.	LOW VALUE OF VERTICAL SCALE, SET BY USER WHEN SVS=1	HIGH VALUE OF VERTICAL SCALE. SET EY USER WHEN SVS=1	NUMBER OF ESTIMATORS THAT WILL BE USED TO CALCULATE STRIISTICAL FARAMETER FROM X DATA. NEST MUST BE 1,2 OR 3.	NAMES OF THE ESTIMATOR FUNCTIONS THAT WILL EE USED TO CAICULATE THE STATISTICAL PARAMETER. CAIL SEQUENCE ON EACH FUNCTION IS: CAIL FNAME(X,N) WHERE X IS THE DATA ARRAY AND N IS THE NUMBER OF DATA PCINTS. THEY MUST BE DECLARED IN THE CALLING ERCGRAM IN THE ORDER THEY ARE USED. DUMMY VARIABIES MUST BE INSERTED WHEN THERE ARE LESS THAN 3 ESTIMATORS.	TITLES ASSOCIATED WITH EACH ESTIMATOR (EST123). A MAX OF 120 CHARACTERS CAN BE USED TO DESCRIEE EACH ESTIMATOR.
		RG	SEI	SVS	YMIN	YEAX	NEST	EEE 800 120 120 120 120 120 120 120 120 120 1	TTI1 TTI2



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SUBROUTINE SIMTB3 (ISEED1, ISEED2, ISEED3, Y N, M, NE, I, D, RG, SEI, SVS, YMIN, YMAX, NEST, GEND1, EST1, TTL1, GEND2, EST2, TTL2, GEND3, EST3, TTL3)
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BY VALUE TO A POSTROPHE
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E MUST BE DECLARED AS REAL*8(1)
VAIUE (WHEN PASSING THE TITLE
MINIMUM OF 120 CHARS. BETWEEN
                                                                                                                                                                                      ၁၅
                                                                                                                                                                                     NEST.EQ.3)
                                                                                                                                                                                                                                                                                                                                      CAL
                                                                                                  REAL ULH (4) Y (200 00), GV (2)
REAL*8 TTL 1 (15), TTL 2 (15), TTL 3 (15)
INTEGER NE (4) RG, SEI SVS, SM
INTEGER D, I, NEST, TEST
EACH TITLE PASSED BY MUST BE A
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                                      STIMATOR W/WIDES
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ED1, N, M, EST1, NE, I, RG, L, ULH, Y, GV, ULH (4)
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MIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ST3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ESTIMATOR.
                                                                                                                                                                                                                                                                                                                                                                                                    D 2 I SEED, N, M, NE (IK), ES
L DELETO (Y, KP, YMAX, YM.
L MAXMIN (Y, KP, YMAX, YM.
H (2)  ULH (2) = YMIN
H (4)  ULH (4) = YMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   MEE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AL
                                                                                                                                                                                                                                                                                                                         ESTIMATOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              L DELETO (Y, KP, YMAX, Y
L MAXMIN (Y, KP, YMAX, Y
H (2) ULH (2) = YMIN
H (4) ULH (4) = YMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       USING FIXED VERTIC ESTIMATOR USED.
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SCAIE FCR 3RD GO TO 40
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FEOCESS BOXFLOTS USCENTINUE CALL PRST (GEND 1/I SEI WEITE (6,101) ULH (2) WRITE (6,102) TTL (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SEI
                                                                                                                                                                                                                                                                                                                                                                                                       GEND
CALL
CALL
ULH
ULH
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CALL
CALL
ULH
ULH
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) G
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IF (NEST III 3) G(

ISEED=ISEED3

DC 30 IK=11

CALL SECEST (GEND

CALL SECEST (GEND

IF (RG.EQ.1) CALL

IF (RG.EQ.1) CALL

IF YMAX GT. ULH

IF YMAX GT. ULH

IF YMAX GT. ULH

IF YMAX GT. ULH

VETURN CALCULATED

CCNT INUE

YMIN=UIH (2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Q
                                                                                                                                                                                                                                                                                                                 (AL 2)
                                                                                                                                                                                                                                                                                                                    FIND VERTICAL
IS FED = IS EEL?
DC 20 IK = 111
CALL SECEST(CALL SECTS(CALL SECEST(CALL SECTS(CALL SECT
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IF (NEST (FND2 I SEED2 N, M, EST2, NE, L, RG, D, ULH, Y, GV)

WRITE (6, 102) TIL (2), ULH (4)

IF (NEST (FND3) I SEED3, N, M, EST3, NE, L, RG, D, ULH, Y, GV)

WRITE (6, 102) TIL (2) TIL (4)

WRITE (6, 102) TIL (3), ULH (4)

WRITE (6, 102) TIL (4)

CALL PRST (GEND3) I SEED3, N, M, NE (1), EST1, Y, KF)

IS ED = IS EE I

CALL SC EST (GEND1 I SEED, N, M, NE (1), EST1, Y, KF)

IF (RG EO 1) CALL MAXMIN (Y, KP, YMAX, YMIN)

ULH (4) = YMAX

CALL PRST (GEND1, I SEED1, N, M, EST1, NE, L, RG, L, ULH, Y, GV)

WRITE (6, 102) TIL (1)

URH (2) = YMAX

CALL PRST (GEND1, I SEED1, N, M, EST1, NE, L, RG, L, ULH, Y, GV)

WRITE (6, 102) TIL (1)

URH (2) = YMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ISED=ISEEL2
CALL SECEST (GEND2 ISEED, N, M, NE (1), EST2, Y, KP)
IF (RG.EQ.1) CALL LELETO (Y, KP, YMAX, YMIN)
IF (RG.NE.1) CALL MAXMIN (Y, KP, YMAX, YMIN)
UIH(2) = YMIN
UIH(4) = YMAX
CALL PRST (GEND2 ISEED2, N, M, EST2, NE, L, RG, D, UIH, Y, GV)
WRITE (6, 101) ULH(2), ULH(4)
IF (NEST GEND2 ISEED2, N, M, EST2, NE, L, RG, D, UIH, Y, GV)
IF (NEST GEND2 ISEED2, N, M, EST2, NE, L, RG, D, UIH, Y, GV)
IF (NEST GEND2 ISEED2, N, M, EST2, NE, L, RG, D, UIH, Y, GV)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FIND VERTICAL SCAIE FCR 3RD ESTIMATOR AND GRAFH.

I SEED = ISEEC3
CALL SECEST (GEND3 ISEED, N, M, NE (1), EST3, Y, KP)
IF (RG * EQ * 1) CALL MAXMIN (Y, KP, YMAX, YMIN)
IF (RG * NE * 1) CALL MAXMIN (Y, KP, YMAX, YMIN)
UIH (2) = YMIN
UIH (4) = YMAX
CALL PRST (GEND3, ISEED3, N, M, EST3, NE, L, RG, D, UIH, Y, GV)
WRITE (6, 101) ULH (2), ULH (4)
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                                                                                                                                                                                                                                                                                                              ,ULH,Y,GV)
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                                     FORMAT (*** WIDE ST Y VALUES FOUND: YMIN=",G10.4,

FCRMAT (1X "VERTICAL SCALE: YMIN = ",F10.4, 18X "YMAX

FCRMAT (*** ERROR... L MUST BE AN INTEGER EFTWEEN 1 A

FCRMAT (*** ERROR... MUST BE AN INTEGER EFTWEEN 1 A

FCRMAT (*** ERROR... N NE(L) MUST BE 1 OR GREATER TO

FCFMAT (*** ERROR... N NE(L) MUST BE 1 OR GREATER TO

FCFMAT (*** ERROR... D MUST BE LESS THAN OR ECUAL TO

FCFMAT (*** WARNING... D MUST BE LESS THAN OR ECUAL TO

FORMAT (*** WARNING... NE ARRAY ELLEMENTS ARE NOT IN

INCREASING SIZE. IF NE(1) IS NOT SMALLEST ELEMENT

MAY CAUSE PCINTS TO FALL OUTSIDE RANGE CF SCALE
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R CF VALUES IN EACH REPLICATION (M*N MUST VECTOR WITH M CONSECUTIVE BATCHES OF N VIOLE SECTION SIZES (MUST BE BETWEEN 1 AND 8)

Y WITH THE L SUBSAMPLE SIZES (MUST BE IN 1 AND 1 A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        RG, RNEK, NUM (10)
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DATA
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EGRESSION ADJUSTED ESTIMATE
ALCULATES ESTIMATES FROM USER DATA US]
ICTS EASIC OR RETRENCHED GRAPH ON LINI
ENDAT = SUEROUTINE NAME TO GENERATE TH
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BAR BLK
000, GV
VT (8)
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A VECTOR WI
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2 FIOT (122,50)
LH(4) DLH(4) Y
H(6,100), STAT(
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REAL*8 SUM2, SUM3, SUM4, LABEL (5)
REAL*4 RA (6,4), RV (8,4), B(4,100), V(4), BA (4), EV (4), BS (4), RT (8), ET (8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      )-UIH(1) * (DLH(3)-DLH(1)) / (ULH(3)-ULH(1)) + DLH(1) +.5
. LAST+4 LOCX(K) = LAST+4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               M REPLICATIONS
                                                                                                                              1. 122. 50 CBAR/11 DOT/ ... KURTCSIS'/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             AND VARIANCE
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NEK=NB(K)

FNEK=NE(K)

SECTION & COMPUTE ESTIMATORS FOR SIZE K

CALL SECEST (GENDAT ISEED, N.M. RNEK, EST Y, KF)

AVERAGE ESTIMATES OF SIZE NE(K) FOR EACH OF

KF=0

EO 10 I=1, R
                                                                                                              LATA DLH/1.1.122.50

DATA BLK/1.1.122.50

DATA LABEL/HEAN' 'STD', STD MEAN', SKEWNESS

IX=18

IX=4

IX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DC S K=1, L

NB(K) = N'NE(K)

IOCX (K) = (NE(K)

IF(LOCX (K) : LT

IAST=IOCX (K) : LT

CCNT INUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         98
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ENOUGH FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           KF / (KP-1.) * (KP-2.))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IS LARGE
RH (K I) = C.

LO 15 J= 1, NB K

K P = KP + 1

G V (1) = A FIN1 (GV (1), Y (KP))

G V (2) = A M AX1 (GV (2), Y (KP))

CONTINUE

EH (K I) = FH (K, I) + Y (KP)

CONTINUE

CONTINUE

X MEAN = O

CONTINUE

X MEAN = S

X MEAN = 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CEECK TO INSURE SAMPLE SIZE

EACH BOME NI COMPUTATION.

IF (KP.LT.2) GO TO 7

VAR = SUM2 / (KP - 1.0)

STDV = SQEI(VAR)

IF (KP.LT.3) GO TO 8

XSUM3 = SNGI(SUM3) * KF / (KP

SKEW = XSUM3 / STDV ** 3

SYUM4 = XSUM4 / SOM 4/ (VAF * VAR)

STAT (K, 2) = STDV / SQRI(FLOAT (KP))

STAT (K, 3) = STDV / SQRI(FLOAT (KP))

STAT (K, 4) = SKEW

STAT (K, 4) = SKEW

STAT (K, 4) = SKEW

STAT (K, 5) = CKURT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ON
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DONE
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              KF / (KP-1.) * (KP-2.))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ENOUGH
                                                                                                                                                                                                                                                                                                                                                                                                                                       COMPUTATION.
FH (K I) = C.

LO (15 J= 1, NBK

K P = KP + 1

G V (1) = A KIN1 (GV (1), Y (KP)

G V (2) = A MAX1 (GV (2), Y (KP)

CONTINUE

FH (K I) = FH (K, I) + Y (KP)

CONTINUE

COMPUTE MEAN AND MCMENT ESTIMATES

WEAN = 0

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

CONTINUE

XMEAN = X MEAN X (I M 1)

SUM = 0 CCO

SUM = 0 CCO

SUM = SUM + DEV * DEV

SUM = SUM + DEV * MEAN

CONTINUE

SUM = SUM + DEV * MEAN

CONTINUE

SUM = SUM + DEV * MEAN

CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                     CEECK TO INSURE SAMPLE SIZE I
EACH BOMENT COMPUTATION.

IF (KF.LT.2) GO TO 7

VAR = SUM2 / (KP - 1.0)

STDV = SQEI(VAR)

SYSUM = SNGI(SUM3) * KF / (KP SNGI)

SKEW = SNGI(SUM3) * KF / (KP SNGI)

SKEW = SNGI(SUM3) * (KP - 2.) * KP + (KF.LT.4) GO TO 8

SYSUM = SNGI(SUM4) * (KP - 2.) * KP + (KF.LT.4) GO TO 9

STAT (K - 1) = XMEAN

STAT (K - 3) = STDV

STAT (K - 3) = STDV

STAT (K - 3) = STDV

STAT (K - 5) = STDV

STAT (K - 5) = STDV

STAT (K - 6) = VAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          0 N
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VARIANCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 2
                                                                                                                                                                                                                                                                                                                                                                                                     DC 98 I=3 INIDTH
MAP I PROPEDEVICE SFACE TO USER SPACE
UX= (I-DLH (1)) * (ULH (3) - ULH (1)) / (DLH (3) - DLH (1)) + ULH (1)
COMPUTE THE Y VAIUE FROM X AND THE REGRESSION COEFFICIENTS.
UY= BA (1)
CO 99 J= 1, L
UY= BA (3+1) / UX**J
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ASYMPTOTE, BETAO AND PLOT ACROSS PLCT.
(1) -UIH(2)) * (DIH(4) -DLH(2)) / (ULH(4) -UIH(2)) + DLH(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                MAP THE Y VALUE FRCM USER SPACE TO DEVICE SPACE J= (UY-ULH(2)) * (DLH(4) - DLH(2)) / (ULH(4) - ULH(2)) + DLH(2) | IF(J : LT : 1 : 0R; J : GT : 50) | GO TO 98 | IF(PLOT(I,J) : E.C. ELK) | PLOT(I,J) = LOT | CONTINUE
                                                                                                                                                                           CALC.
                                                                                                                                                                           ယ
                                                                                                                                                                          REFLICATIONS
                                                                                                                                                                                                                                                                                                                                                                                  ASYMPTOTE
                                                                                                                                                                                                                                                                                                I)/FLOAT(M)
|GO TO 94
|I)-M*BA(I)**2)/(M*(M-1.))
|I)**.5
         IF (D1. LT. 2) GO TO 113

DC 92 K=1 L

CC 47 J=1 L

RT (J)=RH (J,K)

CCNT INUE

CALL RREG (FA, RT, BT, I, D1, IX1, IX2)

E (1 K)=BT (1)

E (2 3 KT=2 D1

E (KT,K)=Ef(KT)*NE(I)**(KT-1)

CCNT INUE
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                                                                                                                                                                          OVE
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                                                                                                                                                                                                                                                                                                                                                                                   ESTABLISH REGRESSION LINE
                                                                                                                                                                          CCEFF.
                                                                                                                                                                                                   DO 94 I=1, L1
EA(I) =0.
EV(I) =0.
CC 95 J=1, M
BA (I) =BA (I) +B(I, J) **2
CONTINUE
EA(I) =BA (I) /F LOA T (M)
IF(M. EQ. 1) GO 94
EV(I) = (BV(I) - M*BA(I) **2)
+ CCNTINUE
                                                                                                                                                                          AVERAGE RECFESSION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALE
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92
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WITH A VARIANCE.
                                                   REGRESSION CN VARIANCES FROM EACH SEGMENT
IF (J . II. 1 . OR. J . GT. 50) GO TO 117

IF (PLCT (I.J) . EQ. BIK) PLOT (I.J) = DASH
                                                                                            DO 111 I=1, I

LT=IT-1

LT=IT-1

LT=IT-1

R= M*(N/NE(LT))

12 IF (LT.LT.DT) DT=LT

IF (DT.IT.2) GO TO 113

DC 48 J=1 I

VT (J) = $TAT (J,6) * (NE(J) **0.5)

VT (J) = $TAT (J,6) * (NE(J) **0.5)

CCNTINUE

CALL REG (FV, VT, V, LT, DT, IX1, IX2)

DC 77 I=1, LT

V (I) = V(I) *NE(L) ** (FLOAT(I) /2.)
                                                                                                                                                                                                                                        ***
                                                                    K=M*(N/NE(I))
I T=L
CT=D1
DO 111 I=1,I
                                                                                                                                                                                                                                        FIOT
                                                                                                                                                                                                                                                                                                                                                                                                          115
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COMPUTE
ТC
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GC TO 14

GC TO 14

IF (D1 Lfr 2) GO TO 444

WRITE (6,151) (BA(I), I=1,D1)

WRITE (6,152) (BV(I), I=1,D1)

WRITE (6,152) (BV(I), I=1,D1)

WRITE (6,152) (BV(I), I=1,D1)

WRITE (6,152) (V(I), I=1,D1)

WRITE (6,152) (V(I), I=1,D1)

FCRMAT (9x, 1,122 A1,1) (+1)
       130
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100
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   THE
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   _{\rm IO}
P75 = PCTL (Y'NY'75'1)
E50 = PCTL (Y'NY'75'1)
IQ2= (P25-YMIN) *VSCALE+1.
IQ3= (P75-YMIN) *VSCALE+1.
IC3= (P75-YMIN) *VSCALE+1.
XIOW= 2*P25-F75
ILOW= (XLOW-P75) *VSCALE+1.
XHI= 2*F75-F25
IHI= (XLOW-P75) *VSCALE+1.
CLCW= 2*F75-F25
CHI= 2*F75-F25
CHI= 2*F75-F25
CHI= 2*F75-F25-F35
CHI= 2*F75-F35-F35
CHI= 2*F75-F35
CHI= 2*F75-F35-F35
CHI= 2*F75-F35
CHI= 2*F75
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = DASH
= DASH
= DASH
= DASH
> UTLIERS
SO TO 55
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IQ3
= CBAR
= CBAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               J= Y (I) - YRIN) + VI (I) - YRIN + VI (I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FLOT (IX-1
FLOT (IX+1
CNT INUE
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DC 31
J= X
IF X
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IF (Y (I) . GE.CLOW . AND.Y (I) . LT.XLOW)
IF (LFIAG . CR. Y (I) . LT.XLOW)
IF (LFIAG . CR. Y (I) . LT.XLOW)
IF LEAST IS THE LOW-CROSS POINTER (1ST POINT GE XLCW)
IIX = J
NEXT LINE ENDS UF WITH HI-CROSS POINTER (IAST FOINT LE
IF (Y (I) . LE.XHI) IHX = J
                                                                                       0
                                                                                                                                                                                                                                                                                                                                                                             ENTRY SCALI(ULH, DLH)
CCMPUTES X, Y SCALE AND LIMITS
XMIN=ULH(1)
                                                                         <del>-</del>
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PRINTED
                                                                                                                           SUEROUTINE FREG(XS, YS, BS, M, N, IX1, IX2)

RCBUST REGFESSION CN Y=X*B

X=M BY N MATRIX CCNTAINED IN AN ARRAY OF DIM (IX1, IX)

Y=M-VECTOR CONTAINED IN AN ARRAY OF DIM (IX1)

XX, XXI=WORK ARRAYS OF DIM (IX2, IX2)

WY=WORK ARRAY OF DIM (IX2, IX2)

XX=WORK MATRIX OF DIM (IX1, IX2)

XY=WORK ARRAYOF DIM (IX2, IX2)

XY=WORK ARRAYOF DIM (IX2)

XY=WORK ARRAYOF DIM (IX2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 В
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              NUMPRT PLOTS THE NUMBER IK IN THE 2-D ARRAY TRE PLOT (IX, J) POSITION.

IX = COLUMN OF MATRIX PLOT WHERE NUMBER IS 3
                                                                                                                                                                                                                                                                     REAL*4 YS(E), XS(B,4), BS(4)

BEAL*8 Y(B), X(B,4), B(4), XTX (4,4), XTY(4)

CCNVERT

Y(I) = DBIE(YS(I))

CONTINUE

X(I,3) = DBLE(XS(I,3))

CCNTINUE
X MAX = UIH { 2 }
Y MIN = UIH { 4 }
Y MAX = UIH { 4 }
HSCALE = { DLH { 4 }
VSCALE = { DLH { 4 }
FFTURN
END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SUBROUTINE NUMPRT (IX, J, IK, PLOT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                    FEAL*8 TO REAL*4
|-1 I X2
|}=$NGL(E(J))
                                                                                                                                                                                                                                                                                                                                                                                                  MATHOI (X Y KTY B, N)
CHOLES (XTX, XTY, B, N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                   CCNVEFT F
DO 15 J=
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                    CALL
                                                                                                                                                                                                                                                                                                                                                                                                                                         C * * * *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ****
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SUBROUTINE SECEST (GENDAT, IX, N, M, NEK, EST, Y, KP)

0000



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2000)
                           (LIMITED TC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CELETO (Y KP YMAX YMIN)
SCALES THE GRAPH TO UPPER (LOWER) QUARTILE +
                                                                                                                                                                                                                                 Z
REAL X (2000), Y (1)
INTEGER IX
CCMPUTE ESTIMATES "EST" FOR SECTION LENGTH NEK (LI
NBK=N/NEK
KF=0
DC 10 I=1 K
KP=0
LO 15 J=1, NBK
KP=KF+1
CALL GENEAT (IX, NEK)
Y (KP) = EST (X, NEK)
Y (KP) = EST (X, NEK)
15 CCNT INUE
RETURN
FETURN
FETURN
FETURN
                                                                                                                                                                                                                 SUEROUTINE MAXMIN (Y. N. YMAX, YMIN)
RETURNS MAX AND MIN VALUES OF VECTOR Y OF LENGTH
FEAL Y (N)
YMAX = Y (1)
YMIN = Y (1)
LC 605 J=1 N
IF (Y (J) - Lf. YMIN) YMIN = Y (J)
CCNTINUE
RETURN
FRETURN
FRETURN
                                                                                                                                                                                                                                                                                                                                                                                                NI
                                                                                                                                                                                                                                                                                                                                                                                FUNCTION POTICY NATIFE OF N VALUES IN WHEN ICE NEW ICE TEATA IS ALREADY SORTED REAL Y(N)

REAL Y(N)

REAL Y(N)

REAL Y(N)

REPRICATION (1)

I = MAXO (1NT (6) (1)

I = MINO (1)

REFINO (1)

REFINO (1)

REFINO (1)

FETURN

FETURN

FETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       UBROUTINE
                                                                                                                            10
                                                                                                                                                                                                                                                                                                                     605
                            C
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```
WILTHIM
                                                                                                            SUBROUTINE CHOIES (XIX,XIY, BHAT, N)
REAL*8 L (4,4), SUM, LT (4,4), XTX (4), XTX (4), BHAT (4), WY (4)
REAL*4 B (4)
INTEGER P
 FOINT
1.5 TIMES INTERQUARTILE DISTANCE OR TO FIRST FOI

REAL Y (KP)
P25 = PCTL (Y, KP. 25.0)
F76 = PCTL (Y, KP. 75.1)
F50 = PCTL (Y, KP. 75.1)
YMIN = 2.5 * P26 - 1.5 * F25
YMAX = 2.5 * P26 - 1.5 * F25
IF (Y (1) · GT · YMIN) YMIN = Y (1)
IF (Y (KP) · LI · YMAX) YMAX = Y (KP)
END
                                                                                                                                                                                                             ****
                                                                                                                       CO
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```
****
II ********
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         XRES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FUILD X-TFANSPOSE IN LT ******
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             C C * * * * * * * MATRIX MULTIPLICATION XT * X = C C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUEROUTINE MATSQ (X, XRES, M, N) REAL * 8 X (8,4), XT (4,8), XRES (4,4), SUM
                                                                                                                                                                                                                                                           * IT * BHAT = WY ****

EHAT (N) = WY (N) / LT (N, N)

DC 8 00 II = 2. N

I = N - II + 1

SUM = 0. 0 CC

DO 750 3 = I. N

SUM = SUM + (BHAT (3) * LT (I. 3))

CONTINUE

BHAT (I) = (WY (I) - SUM) / LT (I. I)
                                                                                                K
                                                                               C *** * * * L G O E I T H M PART 1

C *** * * * L G O E I T H M PART 1

C *** * L G O E I T H M PART 1

I I = I - 1

S U M = 0. O E C

D O 600 J = 1, II

S U M = 0. O E C

O N I N U E

700 C C N I N U E

700 C C N I N U E

700 C C N I N U E
                                                                                                                                                                                                                                                                                                                                                                                                            DC 950 I=1 4
B(I)=SNEI (BHAT (I))
CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    EC 20 I=1 \frac{1}{5} M XI (J I) = X (I , J) CONTINUÉ
   Z
 BUILD L-TRANS ECSE

DC 540 I=1 N

DO 530 J=1, N

IT (IJ) = I (J, I)

540 CCNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *
*
*
                                                                                                                                                                                                                                              **
                                                                                                                                                                                                                                                                                                                                                                                                                            055
                                                                                                                                                                                                                                                                                                                                                                                 600
C
                                                                                                                                                                                                                                                                                                                                                       750
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             10
   C
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***
                                                                                                                                                                                                                                                                                                                                                                                                                     SUBROUTINE SORT (Y,N)
INFIACE SORT USING SHELL ALGORITHM ******
INTEGER GAF
ICGICAL EXCH
                                                                                                                                                       XTX
                                                                                                                                                                         SUBROUTINE RATHUL ( X, Y, XTY, M, N ) REAL *8 Y (8), XT (4, 8), X (8,4), XTY (4), SUM
                                     D I=1 N

2 40 5=1 N

SUM = C.6DO

EO 3 C K = 1 M

SCH = SUM + (XT(I,K) * X(K,J))

CCNTINU E

XRES (I,J) = SUM
                                                                                                                                                         18
                                                                                                                                                                                                                                                                                                  DC 50 I=1 N

SUM = 0. 0 EC

DO 40 J=1, M

SUM = SUM + (XT (I, J) *Y (J))

CONTINUE

XTY (I) = SUM

FETURN

END
                                                                                                                                                      **** MATRIX MULTIPLICATION
                                                                                                                                                                                                                       DC 20 I=1 \\ DO 10 \\ XT (J=1) \\ XT (J=1) \\ CONTINUÉ \\ CCNTINUE
                                                                                                                                                                                                       ***
                   XRES
                                                                                                                                                                                                                                                                        C + * * * * XT * Y = XTY
                                                                                       CCNTINUE
FETURN
END
                     14
                                                                                                                                                                                                      BUILD XT
CCNTINUE
                                     50
                   C***** XT
                                      DC
                                                                                                                                                                                             000
                                                                                                                                                                                                                                                                                                                                                             50
```



```
GAP=(N/2)

10

GAP=(N/2)

EXCH=TRUE.

K=N-GAP
DO 2C0 I=1, K
KK=I+GAP
IF (*NCT*, (Y (I) *GT*Y (KK))) GO TO 100

TEMP=Y(K)
Y(I)=Y(KK)
FX (I)=Y(KK)
FX
```



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